

# 3D view with `pst-vue3d`

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## 1 Presentation

The 3D representation of an object or a landscape is one of the most interesting subject in computer science and have many industrial applications (car and plane design, video game etc...). In a smaller way, one can obtain very didactic realizations using PSTricks with two peculiarities:

- using PostScript ;
- being manageable through L<sup>A</sup>T<sub>E</sub>X.

Package `pst-key` of David CARLISLE allows to write commands with parameters. Using this as an interface, one can observe the result of little modifications of some parameters. Our parameters being here: the position of the watcher, the choice of an solid (cube, sphere etc...) and many other things. I want to signal that

- Regarding 3D representation, one does not forget the package `pst-3d` by Timothy Van Zandt who has used the best part of PostScript. Althought limited to parallel projections, this package allows to draw very interesting 3D figure.<sup>1</sup>
- Thanks to Denis GIROU, i have discovered the package `pst-key` and I have learned it.
- I have written another package for drawing picture reflecting in spherical mirrors.<sup>2</sup>

It is a french paper which illustrate a study of Pr. Henri BOUASSE from this book *Optique supérieure*, edited in 1917 by Delagrave.

## 2 Aims

First, we want to draw the 3D representation with elimination of the hidden parts of some objects.

The position of the watcher will be defined by its spherical coordinates: the distances from the origin, the longitude  $\theta$  and the latitude  $\phi$ .

We will choose, too, the distance of the projection screen from this point.

Second, we want to define some 3D elements of the scene : the bricks.

The following bricks are already defined

- A box given by its three dimensions  $A, B, C$ : it could be turn into a cube or a dice.
- A point which can be defined it two ways
  - By cartesian coordinates  $(x, y, z)$
  - Or by spherical coordinates  $(R, \theta, \phi)$  ( $\theta, \phi$  are, respectively, longitude and latitude).
- A rectangle.
- A circle defined by the normal line to its plane, its center and its radius. An arc is defined as the circle with two limit angles.
- A tetrahedron given by the coordinates of the center of its base and the radius of the circle containing the vertex of each faces. We can make it rotate.
- A square pyramid given by the half of the length of the side of its base and its height. We can make it rotate and move.
- A sphere given by the coordinates of its center `\SphereThreeD(x,y,z){Radius}` and its radius. We can make it rotate with the parameters `RotX=...`, `RotY=...`, `RotZ=...`. We can choose to draw only some meridians and parallel circles.
- A solid or empty half-sphere (same parameters than a sphere)
- A vertical cylinder defined by its radius and its height. We can make it rotate using the parameters `RotX=...`, `RotY=...`, `RotZ=...`. An we can choose the center of its base in the same way than the Sphere.
- A cone and a truncated cone defined by the radius of their base, the height and the height of the truncature.

<sup>1</sup>A lot of different examples for 3D images are available at: <http://members.aol.com/Mluque5130/>

<sup>2</sup><http://melusine.eu.org/syracuse/mluque/BouleMiroir/boulemiroir.html>

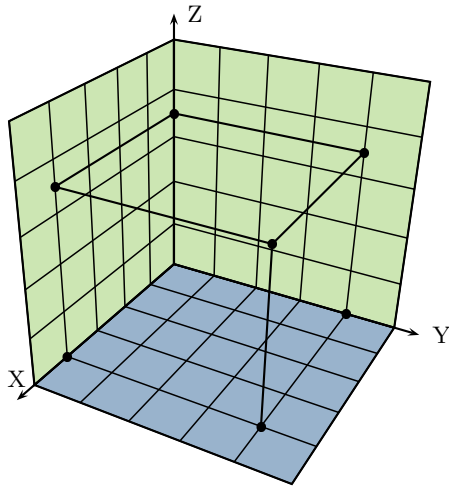


Figure 2: Origin (40,40,35)

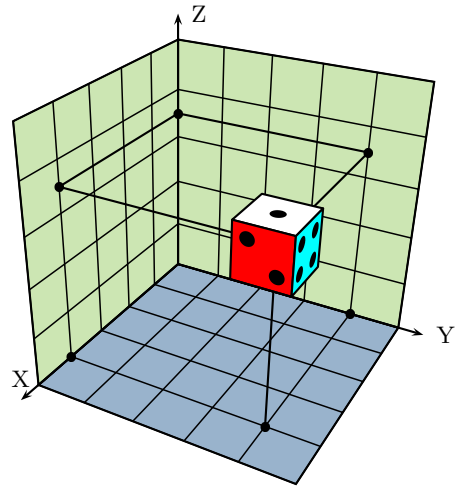


Figure 3: The placed cube.

To construct a scene, one may choose himself the order of the objects. For example, if an object 1 is partially hidden by an object 2, we write, in the list of commands, first object 1 and second object 2.

### 3 Rotating in the 3D space

A 3D object can be rotated around every axes with the `RotX`, `RotY` and `RotZ` option. They can be mixed in every combination. Figure 1 shows how a rotation around the z-axes works.

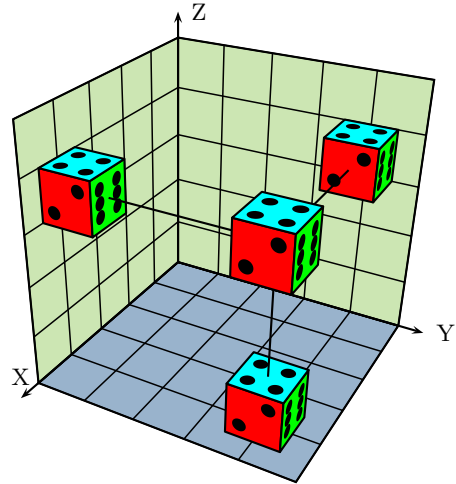


Figure 4: 90° rotation around  $OX$  and plane projections.

```
\begin{pspicture}(-1.5,-1.5)(1.5,1.5)
\psset{THETA=70,PHI=30,Dobs=200,Decran=10}
\psset{A=5,B=5,C=A,fillstyle=solid,%
fillcolor=GrisClair,%
linecolor=red, RotZ=\iRotZ}
\tapis\DieThreeD(0,0,0)%
\LineThreeD[linecolor=red,linestyle=dashed,%
arrows=->](0,0,0)(0,0,25)
\uput[180](Z'){\texttt{RotZ=\iRotZ}}
\end{pspicture}\hfill %
```

### 4 Location of the cube in the space

Suppose that one wants to place a 10-units edge cube at the point ( $x = 40, y = 40, z = 35$ ). First, the half edge of the cube will be define by the parameters :  $A=5, B=5, C=5$ , and next the coordinates of its center by (40,40,35). On the figure, the period of the grid is 10 units (figure 2).

To make it rotate of around  $OX$  , one adds the parameter `RotX=90`(figure 4).

Three successive rotations around three axes with: `RotX=60, RotY=20, RotZ=110`, are illustrate in figure 5.

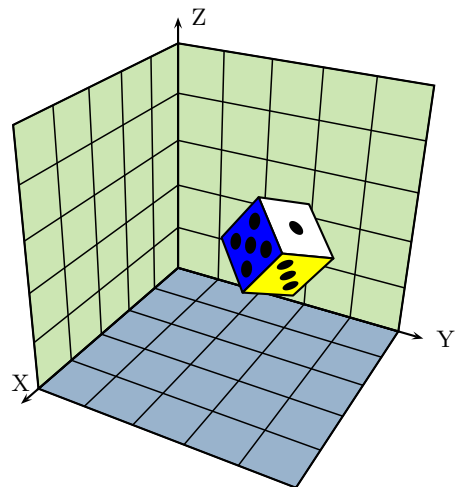


Figure 5: rotations around  $OX$ ,  $OY$  et  $OZ$  : `RotX=60, RotY=20, RotZ=110`.

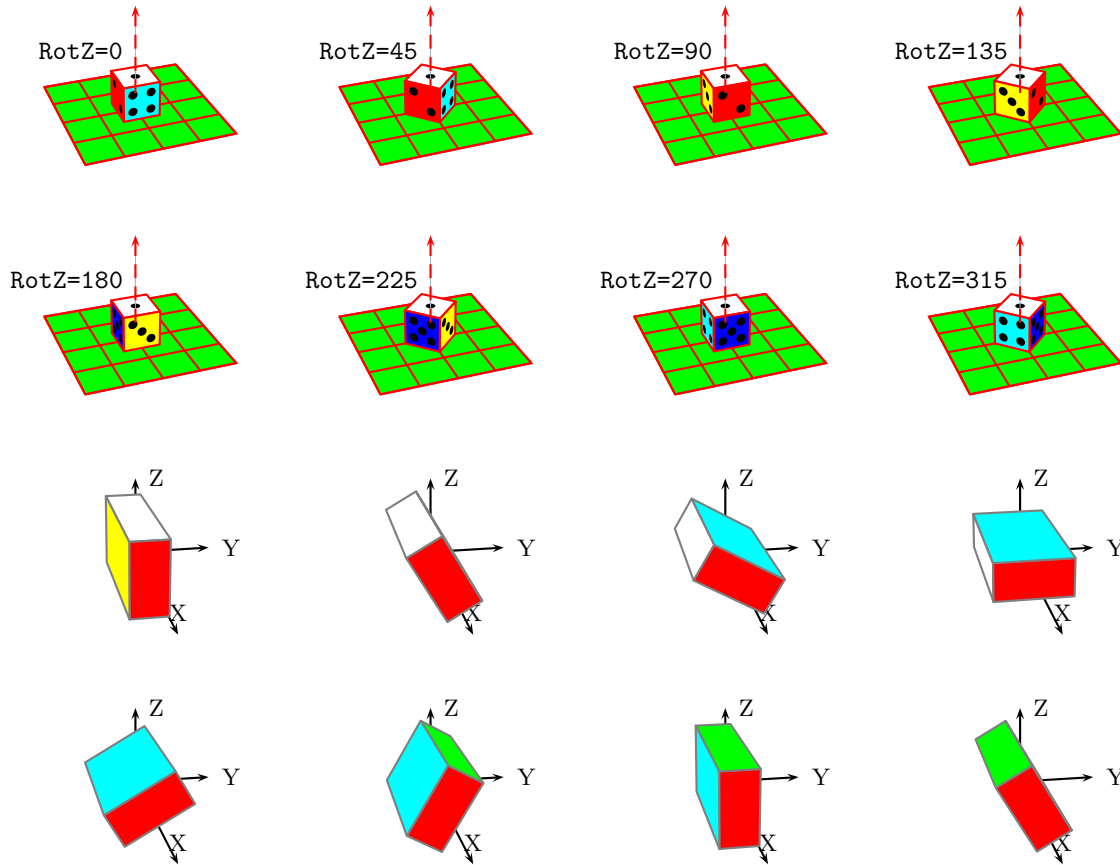


Figure 1: Different views of a die and a cube

## 5 Constructions using cubes

This section was done after a book first published in 1873 and titled:

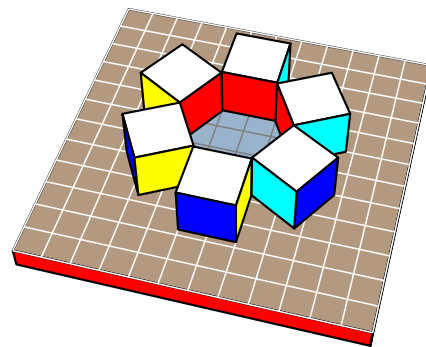
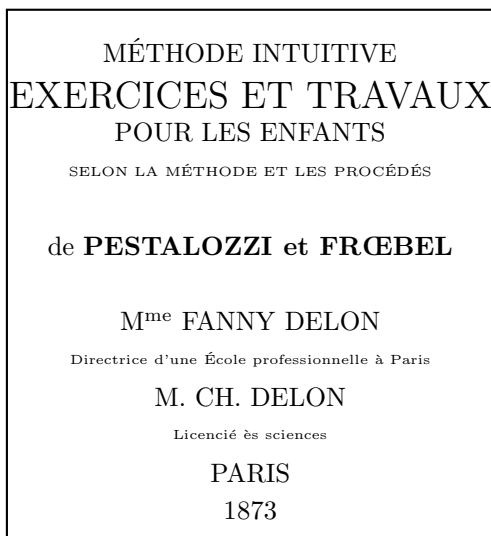


Figure 6: hexagon.

Observing figure from off :

`\psset{PHI=90,THETA=0}`

one obtains classical geometric figures :  
(14) (15) (16) (17) (18) (19) (20) (21).

for children at infant school! One can not be surprised that theses kinds of pedagogue gave rise to the generation of Eintein, Maxwell, Bohr etc.

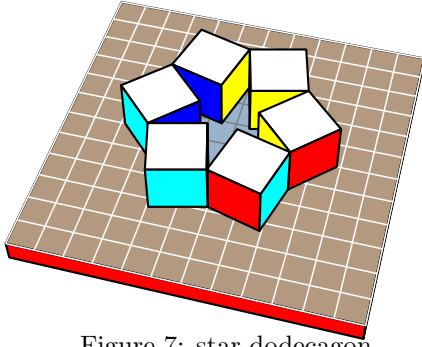


Figure 7: star dodecagon.

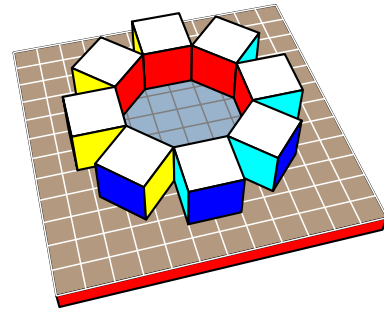


Figure 11: octagon.

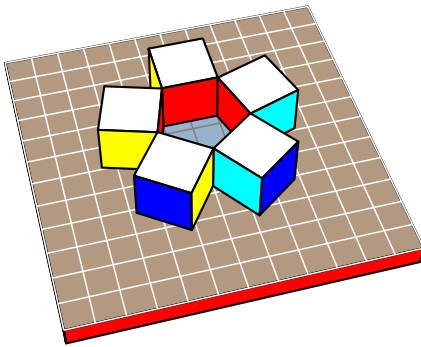


Figure 8: pentagon.

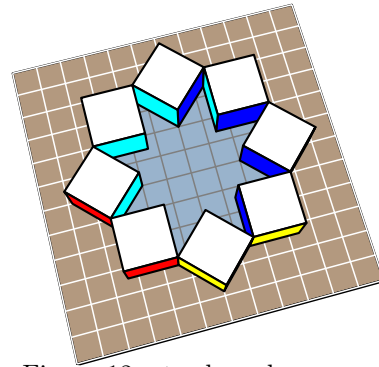


Figure 12: star hexadecagon.

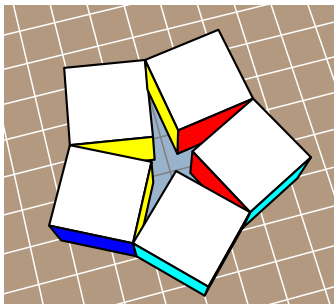


Figure 9: star decagon.

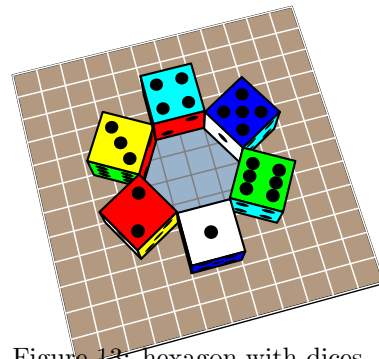


Figure 13: hexagon with dices.

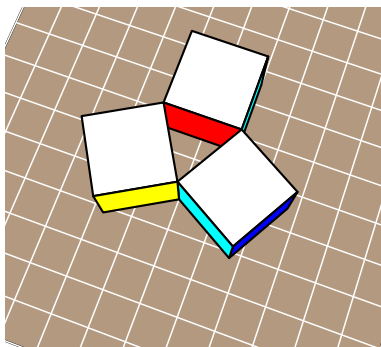


Figure 10: triangle.

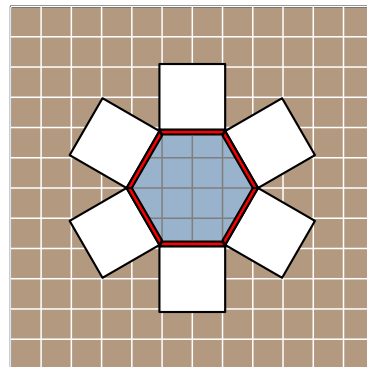


Figure 14: "flat" hexagon.

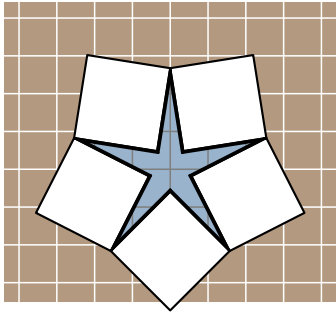


Figure 15: “flat” star dodecagone.

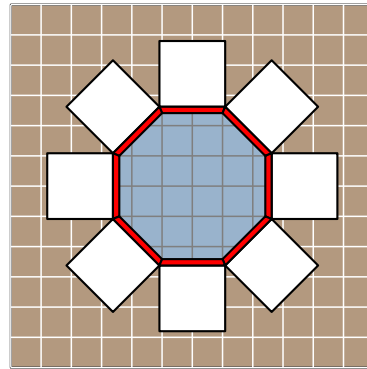


Figure 19: “flat” octogon.

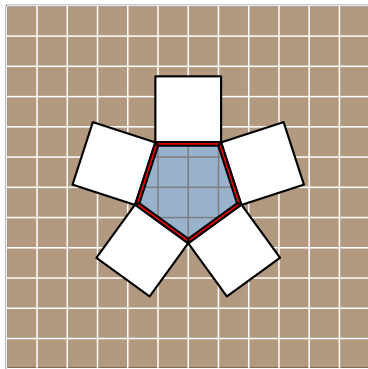


Figure 16: “flat” pentagon.

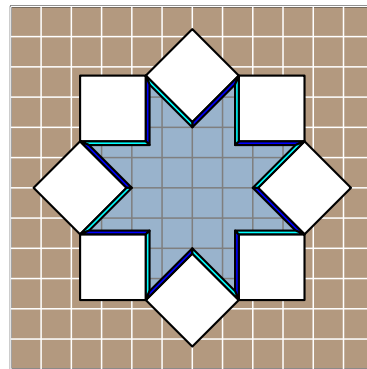


Figure 20: “flat” star hexadecagon.

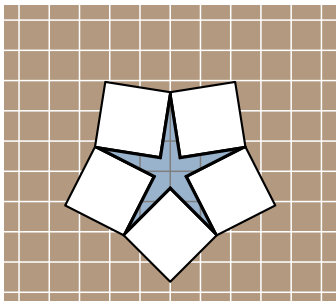


Figure 17: “flat” star decagon.

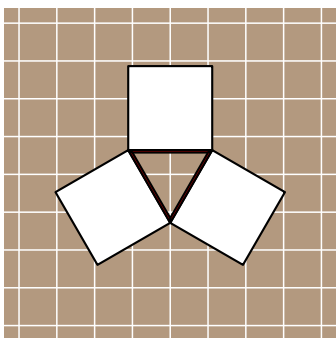


Figure 18: “flat” triangle.

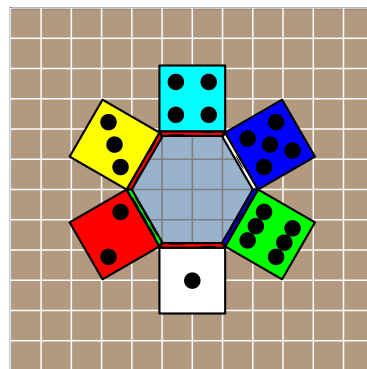


Figure 21: “flat” hexagon with dices.

## 6 Sphere, part of sphere, half-sphere, parallels and meridians

Beside `sphereThreeD` there exist several macro for spheres:

- `SphereInverseThreeD`
- `\SphereCercleThreeD`
- `\SphereMeridienThreeD`
- `\DemiSphereThreeDThreeD`
- `\SphereCreuseThreeD`
- `\PortionSphereThreeD`

The macro:

```
\SphereThreeD(10,30,20){20}
```

draws the sphere defined by the coordinates of its centre and its radius which is shown in figure 22 together with the macro

```
\PortionSphereThreeD(0,0,0){20}
```

and some more additional lines.

```
\begin{pspicture}(-3,-3.5)(3,5)
\psset{THETA=30,PHI=30,Dobs=100,Decran=10}
{\psset{style=GradGrayWhite}%
\SphereThreeD(0,0,0){20}
\psset{fillstyle=solid,fillcolor=gray}
\PortionSphereThreeD(0,0,0){20}
\pNodeThreeD(20;10;10){C1}
\pNodeThreeD(40;10;10){D1}
\psline(C1)(D1)
\pNodeThreeD(20;10;-10){C2}
\pNodeThreeD(40;10;-10){D2}
\psline(C2)(D2)
\pNodeThreeD(20;-10;-10){C3}
\pNodeThreeD(40;-10;-10){D3}
\psline(C3)(D3)
\pNodeThreeD(20;-10;10){C4}
\pNodeThreeD(40;-10;10){D4}
\psline(C4)(D4)
\PortionSphereThreeD%
[style=GradGrayWhite](0,0,0){40}
% PhiCercle=latitude of the cercle
% \SphereCercle[PhiCercle=...]{radius}
\psset{linecolor=white,PhiCercle=45}
\SphereCercleThreeD(0,0,0){20}
% ThetaMeridien=longitude of the meridian
% \SphereMeridien[ThetaMeridien=...]{radius}
\SphereMeridienThreeD%
[ThetaMeridien=45](0,0,0){20}
\pNodeThreeD(20;45;45){A}
\pNodeThreeD(50;45;45){B}
\psline[linecolor=black]{->}(A)(B)
\pNodeThreeD(20;0;90){Nord}
\pNodeThreeD(40;0;90){Nord1}
\psline[linecolor=black]{->}(Nord)(Nord1)
\SphereCercleThreeD[PhiCercle=0](0,0,0){20}
\SphereMeridienThreeD%
[ThetaMeridien=0](0,0,0){20}
\end{pspicture}
```

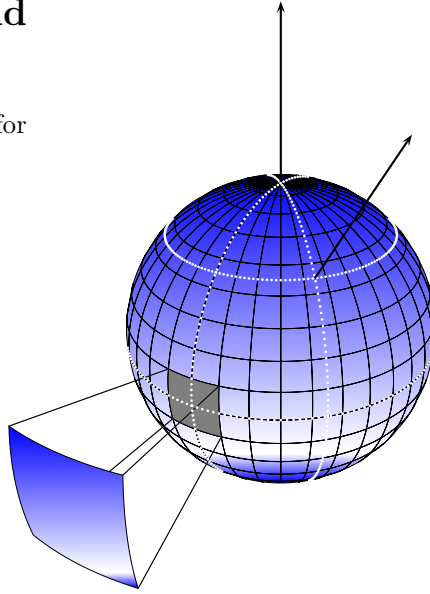


Figure 22: A Sphere.

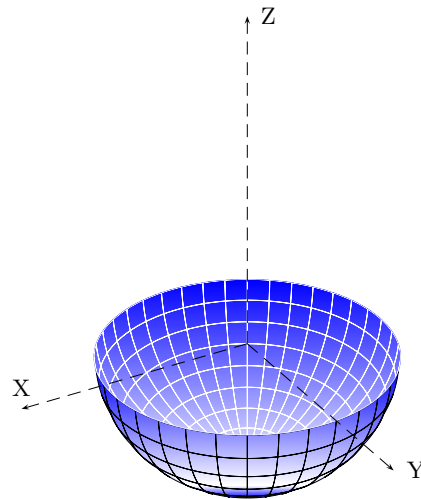


Figure 23: half-sphere.

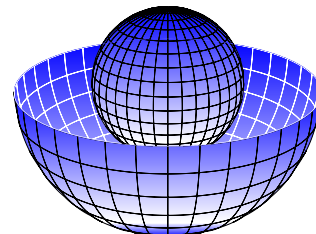


Figure 24: levitation

## 7 A Hole in a sphere

It is a rectangular hole whose size are meridian and parallels arcs (figure 25).

We define the part of the sphere setting its

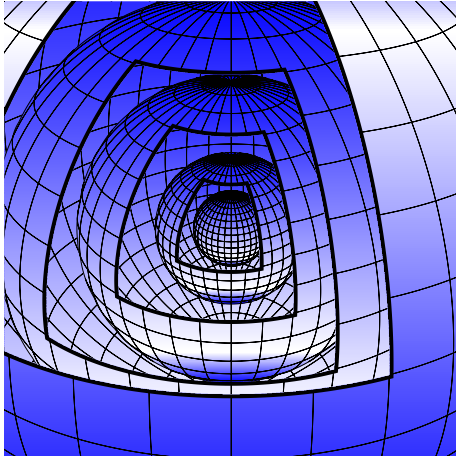


Figure 25: A Hole in a sphere.

radius, the center of the sphere and the  $\Delta\phi$  and  $\Delta\theta$ .

```
\PortionSphereThreeD[PortionSpherePHI=45,%
    PortionSphereTHETA=0,%
    DeltaPHI=45,%
    DeltaTHETA=20](0,0,0){20}
```

There are the parameters of the first hole. The radius is 20.

```
{\psset{fillstyle=gradient,%
    gradbegin=white,%
    gradend=blue,%
    gradmidpoint=0.2,%
    linecolor=cyan,%
    linewidth=0.1mm}
\SphereThreeD(0,0,0){20}}%
\begin{psclip}{%
\PortionSphereThreeD[PortionSpherePHI=45,%
    DeltaPHI=45,DeltaTHETA=20](0,0,0){20}}
\SphereInverseThreeD[fillstyle=solid,%
    fillcolor=red,%
    linecolor=blue](0,0,0){20}%
\end{psclip}%
```

This is the tricks to see the inner of the sphere.

`\SphereInverse` define the hidden part of the sphere.

## 8 Drawing a cylinder

A cylinder is defined by the radius of its base and its height. The center of the base is set in the usual way, and `RotX, RotY, RotZ` make it rotate around the axes.

```
\CylindreThreeD(x,y,z){radius}{hauteur}

\CylindreThreeD(0,0,-5){10}{15}}
\psset{RotY=90}
\CylindreThreeD(15,15,-5){5}{20}
```

## 9 Tetrahedron, cone and square pyramid

### 9.1 square pyramid

```
\psset{A=...,Hpyramide=...}
```

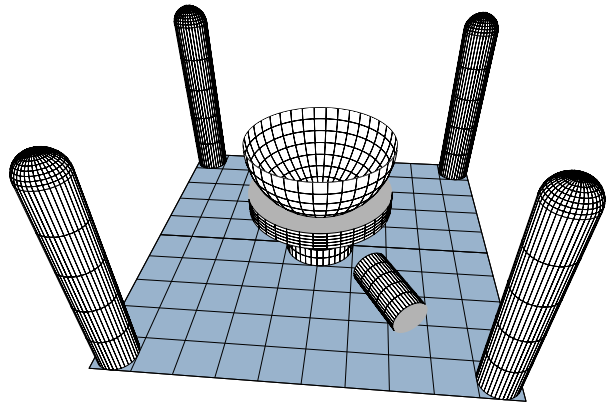


Figure 26: cylinders.

`\Pyramide`

See the examples of figures (27) (28).

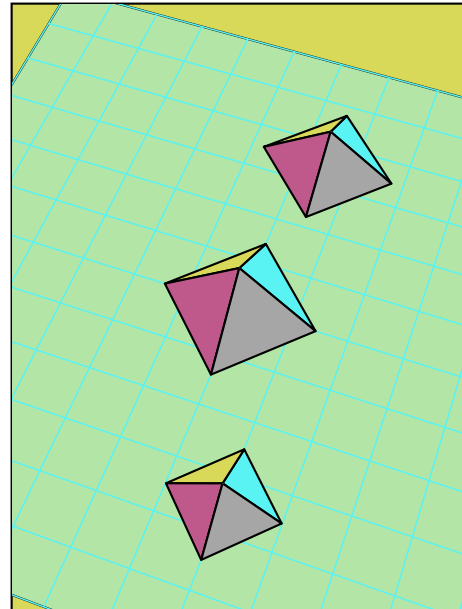


Figure 27: Pyramids of Egypt.

### 9.2 Cone

```
\ConeThreeD[fracHeight=...]
    (x,y,z){radius}{Height}
```

by default `fracHeight=1` : figure 29.

## 10 Points and lines

The command allowing to mark points and thus to draw lines and polygons can be used of two manners, either with the Cartesian coordinates

```
\pNodeThreeD(x,y,z){name}
```

or with the spherical coordinates :



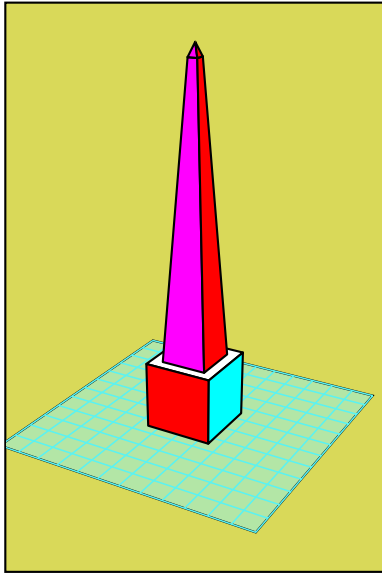


Figure 28: Obelisk of Egypt.

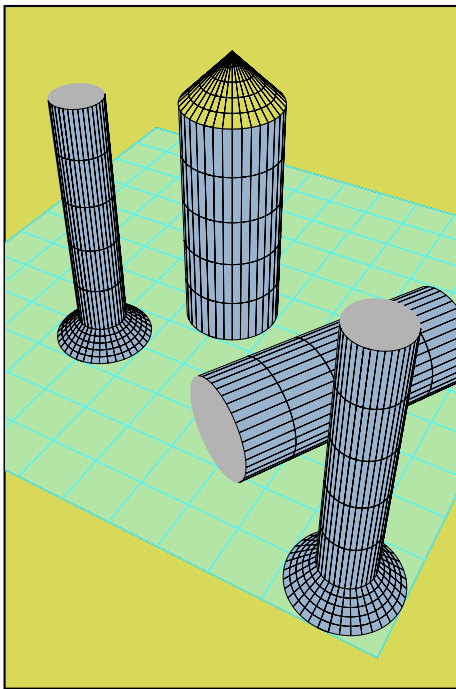


Figure 29: Cones and cylinders.

```
\pNodeThreeD(radius;longitude;latitude)%
      {name of the point}
```

For example `\pNodeThreeD(25,-25,25){A}`, the point  $A(25, 25, 25)$  places. Points being positioned, just to write `\psline(A)(B)`, to draw the segment  $AB$ .

On the figure 30, one drew a cube with its diagonals.

## 11 Circles

A circle is defined by a vector normal for its plan by  $(\theta, \varphi)$ , with the following parameters for example:

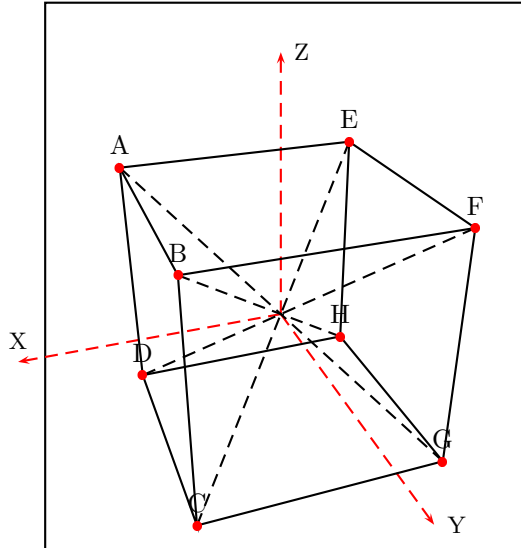


Figure 30: Points and lines.

```
normaleLongitude=60,normaleLatitude=90
```

The coordinates of his centre as well as his radius.

```
\CircleThreeD(x,y,z){radius}
```

The circles of the figure 31, were drawn with the following commands:

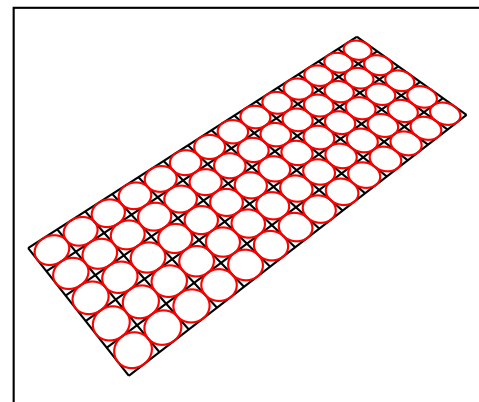


Figure 31: circles.

```
\psset{normaleLongitude=0,%
      normaleLatitude=90}
\multido{\iXorigine=-65+10}{14}{%
  \multido{\iYorigine=5+10}{5}{%
    \CircleThreeD[linecolor=red]%
      (\iXorigine,\iYorigine,0){5}}}
```

## 12 The macros and the options

### 12.1 The colors of the cube, the pyramid and tetraedre

The predefined colors for the different sides of a cube are always set in the `rgb` mode :



```

CubeColorFaceOne=1 1 0,%
CubeColorFaceTwo=0.9 0.9 0,%
CubeColorFaceThree=0.8 0.8 0,%
CubeColorFaceFour=0.7 0.7 0,%
CubeColorFaceFive=0.65 0.65 0,%
CubeColorFaceSix=0.75 0.75 0

```

The colors for the pyramid and the tetraedre are taken from the predefined ones:

```

ColorFaceD=cyan,
ColorFaceA=magenta,
ColorFaceB=red,
ColorFaceC=blue,
ColorFaceE=yellow

```

They can be changed in the usual way with the `\psset` macro.

## 12.2 Common parameters

`RotX=<value>`, `RotY=<value>`, `RotZ=<value>`

The predefined value is zero, means no rotation.

## 12.3 Cube

The following command places a parallelepiped with a length of  $a = 40$ ,  $b = 20$  and  $c = 10$  units and it is placed with its center at the point  $x = 25$ ,  $y = 25$  and  $z = 25$

```
\CubeThreeD[A=20,B=10,C=5](25,25,25)
```

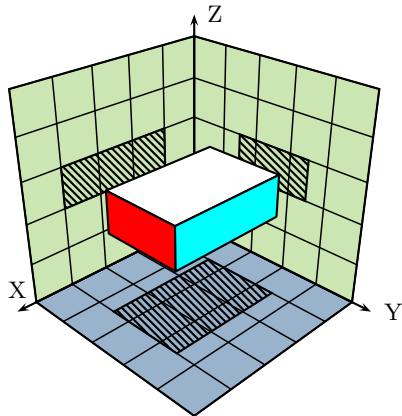


Figure 32: Parallelepiped

In other words: the length of the sides is  $2A, 2B, 2C$  (see figure 32).

For rotations, let us consider the result of a rotation around one of the axes, while knowing that it is possible to combine them. The corresponding rotation of projection on the horizontal level is obtained with the parameter: `normaleLongitude=<degrees>` (figure 33).

There is no difference to a die, except that all sides have the same length.

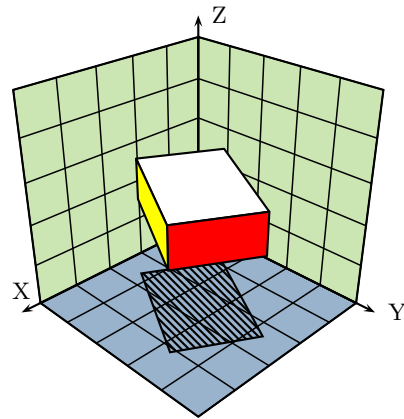


Figure 33: The same parallelepiped rotated with `RotZ=60`.

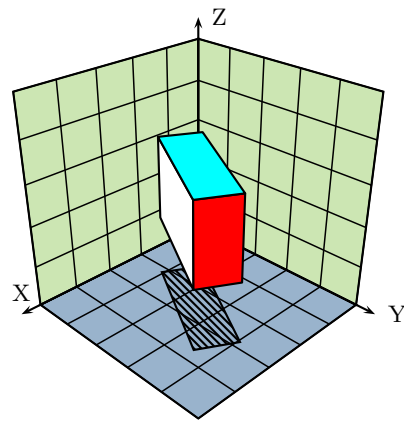


Figure 34: The same parallelepiped, rotated with the values `RotX=90, RotZ=60`

## 12.4 Cylinder and circle

In addition to the already quoted optional parameters the cylinder requires the obligatory parameters:

```
\CylindreThreeD[...](x,y,z){radius}{height}
```

Projection on the horizontal level is obtained with the following values:

```

\CircleThreeD[normaleLongitude=0,%
normaleLatitude=90,%
fillstyle=vlines,%
hatchsep=0.4mm](30,30,0){10}

```

The circle macro needs the following parameters:

```
\CircleThreeD[...](x,y,z){radius}
```

Figure 35 shows an example of the above macros.

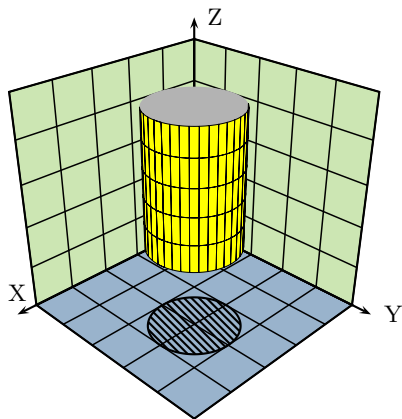


Figure 35: A cylinder with a radius of 10 units and a height of 50 units with its base center at  $(30, 30, 20)$ .

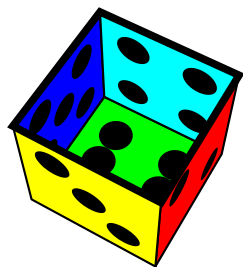


Figure 36: An empty box.

## 13 See the interior of a cube

The following option makes it possible to visualize the interior of the box, the result is seen in the figure 36 :

```
\DieThreeD(0,0,0)%
\begin{psclip}{%
\FrameThreeD[normaleLongitude=0,%
normaleLatitude=90]%
(0,0,10)(-10,-10)(10,10)}%
\DieThreeD[CubeInside=true](0,0,0)%
\end{psclip}%
```

## 14 Another package about the 3D

Concerning 3D and PSTricks, I indicate package of Herbert VOSS (`pst-3dplot`), rather dedicated towards the representation of the mathematical functions.