$\begin{array}{c} \text{prooftrees} \\ \text{Version v0.9 (SVN Rev: 10525)} \\ \text{Clea F. Rees}^* \\ 2024/10/24 \end{array}$

Abstract

proof trees is a LATEX 2ε package, based on forest, designed to support the typesetting of logical tableaux — 'proof trees' or 'truth trees' — in styles sometimes used in teaching introductory logic courses, especially those aimed at students without a strong background in mathematics. One textbook which uses proofs of this kind is Hodges (1991). Like forest, prooftrees supports memoize out-of-the-box.

Note that this package requires version 2.1 (2016/12/04) of forest (Živanović 2016). It will not work with versions prior to 2.1.

I would like to thank Živanović both for developing forest and for considerable patience in answering my questions, addressing my confusions and correcting my mistakes. The many remaining errors are, of course, entirely my own. This package's deficiencies would be considerably greater and more numerous were it not for his assistance.

$S \leftrightarrow \neg T, T \leftrightarrow \neg R \mid_{\mathcal{L}} S \leftrightarrow R$		$(\exists x)$	$((\forall y)(Py \Rightarrow (x = y)) \cdot Px) \Big _{\mathcal{L}_1} (\exists x)(\forall y) \Big _{\mathcal{L}_1} (\forall y) \Big _{\mathcal{L}_1} (\forall y) \Big _{\mathcal{L}_1} (\exists x)(\forall y) \Big _{\mathcal{L}_1} (\forall y) \Big _{\mathcal{L}_1}$	$(\forall y)(Py \Leftrightarrow (x=y))$
1. $S \leftrightarrow \neg T \checkmark$	pr.	1.	$(\exists x)((\forall y)(Py \Rightarrow (x = y)) \cdot Px) \checkmark d$	pr.
2. $T \leftrightarrow \neg R \checkmark$	pr.	2.	$\sim (\exists x)(\forall y)(Py \Leftrightarrow (x=y)) \setminus d$	\neg conc.
3. $\neg(S \leftrightarrow R) \checkmark$	\neg conc.	3.	$(\forall y)(Py \Rightarrow (d=y)) \cdot Pd \checkmark$	$1 \exists E$
		4.	$(\forall y)(Py \Rightarrow (d=y)) \ \backslash c$	$3 \cdot E$
4 S $\neg S$	$1 \leftrightarrow E$	5.	Pd	$3 \cdot E$
$5 \qquad \neg T \qquad \neg \neg T \checkmark$	$1 \leftrightarrow E$	6.	${\sim}(\forall y)(Py \Leftrightarrow (d=y)) \checkmark c$	$2 \sim \exists E$
		7.	$\sim (Pc \Leftrightarrow (d=c)) \checkmark$	$6 \sim \forall E$
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	$2 \leftrightarrow E$	8.	\overrightarrow{Pc} $\sim Pc$	$7 \sim \Leftrightarrow E$
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	$Z \leftrightarrow \mathbb{E}$	9.	$d \neq c$ $d = c$	$7 \sim \Leftrightarrow E$
		10.	Pc	5,9 =
8. $\neg S$ S $\neg S$ S T	$3 \neg \leftrightarrow \mathbf{E}; 5 \neg \neg \mathbf{E}$	11.	$Pc \Rightarrow (d = c) \checkmark \otimes$	$4 \forall E$
9. $R \neg R R \neg R \otimes$	$3 \neg \leftrightarrow \mathbf{E}$		8,10	
10. \otimes R \otimes \otimes 6,8	7 ¬¬ E	10		11 V D
$4,8 \otimes 7,9 4,8$		12.	$\sim Pc$ $a = c$	$\Pi \Rightarrow E$
9,10		13.	$\bigotimes a \neq a$	9,12 =
			0,12 ×	
			61	

*Bug tracker: codeberg.org/cfr/prooftrees/issues | Code: codeberg.org/cfr/prooftrees | Mirror: github.com/cfr42/ prooftrees

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1 Raison d'être

Suppose that we wish to typeset a typical proof tree demonstrating the following entailment

 $\{P \lor (Q \lor \neg R), P \to \neg R, Q \to \neg R\} \models \neg R$

We start by typesetting the tree using forest's default settings (box 1) and find our solution has several advantages: the proof is specified concisely and the code reflects the structure of the tree. It is relatively straightforward to specify a proof using forest's bracket notation, and the spacing of nodes and branches is automatically calculated.

Despite this, the results are not quite what we might have hoped for in a proof tree. The assumptions should certainly be grouped more closely together and no edges (lines) should be drawn between them because these are not steps in the proof — they do not represent inferences. Preferably, edges should start from a common point in the case of branching inferences, rather than there being a gap.

Moreover, proof trees are often compacted so that *non-branching* inferences are grouped together, like assumptions, without explicitly drawn edges. Although explicit edges to represent non-branching inferences are useful when introducing students to proof trees, more complex proofs grow unwieldy and the more compact presentation becomes essential.

Furthermore, it is useful to have the option of *annotating* proof trees by numbering the lines of the proof on the left and entering the justification for each line on the right.

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forest is a powerful and flexible package capable of all this and, indeed, a good deal more. It is not enormously difficult to customise particular trees to meet most of our desiderata. However, it is difficult to get things perfectly aligned even in simple cases, requires the insertion of 'phantom' nodes and management of several sub-trees in parallel (one for line numbers, one for the proof and one for the justifications). The process requires a good deal of manual intervention, trial-and-error and hard-coding of things it would be better to have $IATEX 2_{\varepsilon}$ manage for us, such as keeping count of lines and line references.

prooftrees aims to make it as easy to specify proof trees as it was to specify our initial tree using forest's default settings. The package supports a small number of options which can be configured to customise the output. The code for a prooftrees proof tree is shown in box 2, together with the output obtained using the default settings.

More extensive configuration can be achieved by utilising forest (Živanović 2016) and/or TikZ (Tantau 2015) directly. A sample of supported proof tree styles are shown in box 3. The package is **not** intended for the typesetting of proof trees which differ significantly in structure.







2 Assumptions & Limitations

prooftrees makes certain assumptions about the nature of the proof system, \mathcal{L} , on which proofs are based.

• All derivation rules yield equal numbers of *wffs* on all branches.



If \mathcal{L} fails to satisfy this condition, **prooftrees** is likely to violate the requirements of affected derivation rules by splitting branches 'mid-inference'.

- No derivation rule yields *wffs* on more than two branches.
- All derivation rules proceed in a downwards direction at an angle of -90° i.e. from north to south.
- Any justifications are set on the far right of the proof tree.
- Any line numbers are set on the far left of the proof tree.
- Justifications can refer only to earlier lines in the proof. prooftrees can typeset proofs if \mathcal{L} violates this condition, but the cross-referencing system explained in section 7.2 cannot be used for affected justifications.

proof trees does not support the automatic breaking of proof trees across pages. Proof trees can be manually broken by using line no shift with an appropriate value for parts after the first (section 7.1). However, horizontal alignment across page breaks will not be consistent in this case.

In addition, prooftrees almost certainly relies on additional assumptions not articulated above and certainly depends on a feature of forest which its author classifies as experimental (do dynamics).

3 Typesetting a Proof Tree

After loading **prooftrees** in the document preamble:

```
% in document's preamble 
\usepackage{prooftrees}
```

the **prooftree** environment is available for typesetting proof trees. This takes an argument used to specify a $\langle tree \ preamble \rangle$, with the body of the environment consisting of a $\langle tree \ specification \rangle$ in forest's notation. The $\langle tree \ preamble \rangle$ can be as simple as an empty argument — $\{\}$ — or much more complex.

Customisation options and further details concerning loading and invocation are explained in section 4, section 5, section 6, section 7 and section 8. In this section, we begin by looking at a simple example using the default settings.

Suppose that we wish to typeset the proof tree for

$$(\exists x)((\forall y)(Py \to x = y) \land Px) \vdash (\exists x)(\forall y)(Py \leftrightarrow x = y)$$

and we would like to typeset the entailment established by our proof at the top of the tree. Then we should begin like this:

```
\begin{tableau}
  {
    to prove={(\exists x)((\forall y)(Py \lif x = y) \land Px) \sststile{}{} (\exists x)(\forall y)(
    Py \liff x = y)}
    }
    \end{tableau}
```



That is all the preamble we want, so we move onto consider the $\langle tree \ specification \rangle$. forest uses square brackets to specify trees' structures. To typeset a proof, think of it as consisting of nested trees, trunks upwards, and work from the outside in and the trunks down (box 4).

Starting with the outermost tree 12 and the topmost trunk, we replace the \bigcirc with square brackets and enter the first *wff* inside, adding just=Pr. for the justification on the right and checked=a so that the line will be marked as discharged with a substituted for x. We also use forest's name to label the line for ease of reference later. (Technically, it is the node rather than the line which is named, but, for our purposes, this doesn't matter. forest will create a name if we don't specify one, but it will not necessarily be one we would have chosen for ease of use!)

```
\begin{tableau}
  {
    to prove={(\exists x)((\forall y)(Py \lif x = y) \land Px) \sststile{}{} (\exists x)(\forall y)(
Py \liff x = y)}
  }
  [{(\exists x)((\forall y)(Py \lif x = y) \land Px)}, checked=a, just=Pr., name=pr
  ]
  \end{tableau}
```

We can refer to this line later as pr.

We then consider the next tree 12. Its \bigcirc goes inside that for 12, so the square brackets containing the next *wff* go inside those we used for 12. Again, we add the justification with just, but we use subs=a rather than checked=a as we want to mark substitution of *a* for *x* without discharging the line. Again, we use name so

that we can refer to the line later as neg conc.

```
\begin{tableau}
  {
    to prove={(\exists x)((\forall y)(Py \lif x = y) \land Px) \sststile{}{} (\exists x)(\forall y)(
    Py \liff x = y)}
  }
  [{(\exists x)((\forall y)(Py \lif x = y) \land Px)}, checked=a, just=Pr., name=pr
    [{\lnot (\exists x)(\forall y)(Py \liff x = y)}, subs=a, just=Conc.~neg., name=neg conc
    ]
  ]
  \end{tableau}
```

Turning to tree 12, we again note that its \bigcirc is nested within the previous two, so the square brackets for its *wff* need to be nested within those for the previous *wffs*. This time, we want to mark the line as discharged without substitution, so we simply use checked without a value. Since the justification for this line includes mathematics, we need to ensure that the relevant part of the justification is surrounded by \dots or (\dots) . This justification also refers to an earlier line in the proof. We could write this as just=1 ϵ . To do this, we put the reference, pr *after* the rest of the justification, separating the two parts by a colon i.e. $\epsilon = \pi d$ allow prooftrees to figure out the correct number.

```
\begin{tableau}
{
    to prove={(\exists x)((\forall y)(Py \lif x = y) \land Px) \sststile{}{} (\exists x)(\forall y)(
Py \liff x = y)}
}
[{(\exists x)((\forall y)(Py \lif x = y) \land Px)}, checked=a, just=Pr., name=pr
[{\lnot (\exists x)(\forall y)(Py \liff x = y)}, subs=a, just=Conc.~neg., name=neg conc
[{(\forall y)(Py \liff a = y) \land Pa}, checked, just=$\exists\elim$:pr
]
]
\end{tableau}
```

Continuing in the same way, we surround each of the *wffs* for (12, (12, (12), (12), (12), (12)) within square brackets nested within those surrounding the previous *wff* since each of the trees is nested within the previous one. Where necessary, we use name to label lines we wish to refer to later, but we also use forest's *relative* naming system when this seems easier. For example, in the next line we add, we specify the justification as just=land\elim\$:!u. ! tells forest that the reference specifies a relationship between the current line and the referenced one, rather than referring to the other line by name. !u refers to the current line's parent line — in this case, {(\forall y)(Py \lif a = y) \land Pa}, checked, just=\$\exists\elim\$:pr. !uu refers to the current line's parent line and so on.

```
\begin{tableau}
       ſ
               to prove={(|x| x = y| | x = 
Py  \lim x = y 
       }
        [{(\exists x)((\forall y)(Py \lif x = y) \land Px)}, checked=a, just=Pr., name=pr
                 [{\lnot (\exists x)(\forall y)(Py \liff x = y)}, subs=a, just=Conc.~neg., name=neg conc
                         [{(\forall y)(Py \lif a = y) \land Pa}, checked, just=$\exists\elim$:pr
                                 [{(\forall y)(Py \lif a = y)}, subs=b, just=$\land\elim$:!u, name=mark
                                         [Pa, just=$\land\elim$:!uu, name=simple
                                                 [{\lnot (\forall y)(Py \liff a = y)}, checked=b, just=$\lnot\exists\elim$:neg conc
                                                         [{\lnot (Pb \liff a = b)}, checked, just=$\lnot\forall\elim$:!u
                                                        ]
                                                1
                                       ]
                               ]
```

]] \end{tableau}

Reaching 12, things get a little more complex since we now have not one, but two \bigcirc nested within 12. This means that we need two sets of square brackets for 12 — one for each of its two trees. Again, both of these should be nested within the square brackets for 12 but neither should be nested within the other because the trees for the two branches at 12 are distinct.

```
\begin{tableau}
 {
    to prove={(\exists x)((\forall y)(Py \lif x = y) \land Px) \sststile{}{} (\exists x)(\forall y)(
Py  \lim x = y 
 7
 [{(\exists x)((\forall y)(Py \lif x = y) \land Px)}, checked=a, just=Pr., name=pr
    [{\lnot (\exists x)(\forall y)(Py \liff x = y)}, subs=a, just=Conc.~neg., name=neg conc
      [{(\forall y)(Py \lif a = y) \land Pa}, checked, just=$\exists\elim$:pr
        [{(\forall y)(Py \lif a = y)}, subs=b, just=$\land\elim$:!u, name=mark
          [Pa, just=$\land\elim$:!uu, name=simple
            [{\lnot (\forall y)(Py \liff a = y)}, checked=b, just=$\lnot\exists\elim$:neg conc
              [{\lnot (Pb \liff a = b)}, checked, just=$\lnot\forall\elim$:!u
                [Pb, just=$\liff\elim$:!u, name=to Pb or not to Pb
                ]
                [\lnot Pb
                ٦
              ٦
            ]
         ]
       ]
     ]
   ]
 ]
\end{tableau}
```

At this point, we need to work separately or in parallel on each of our two branches since each constitutes its own tree. Turning to trees 12, each needs to be nested within the relevant tree 12, since each \bigcirc is nested within the applicable branch's tree. Hence, we nest square brackets for each of the *wffs* at 12 within the previous set.

```
\begin{tableau}
 {
    to prove={(\exists x)((\forall y)(Py \lif x = y) \land Px) \sststile{}{} (\exists x)(\forall y)(
Py  \lim x = y 
 }
 [{(\exists x)((\forall y)(Py \lif x = y) \land Px)}, checked=a, just=Pr., name=pr
    [{\lnot (\exists x)(\forall y)(Py \liff x = y)}, subs=a, just=Conc.~neg., name=neg conc
      [{(\forall y)(Py \lif a = y) \land Pa}, checked, just=$\exists\elim$:pr
        [{(\forall y)(Py \lif a = y)}, subs=b, just=$\land\elim$:!u, name=mark
          [Pa, just=$\land\elim$:!uu, name=simple
            [{\lnot (\forall y)(Py \liff a = y)}, checked=b, just=$\lnot\exists\elim$:neg conc
              [{\lnot (Pb \liff a = b)}, checked, just=$\lnot\forall\elim$:!u
                [Pb, just=$\liff\elim$:!u, name=to Pb or not to Pb
                 [a \neq b, just=$\liff\elim$:!u
                 ]
                ٦
                [\lnot Pb
                 [{a = b}]
                 ٦
```



We only have one tree 12 as there is no corresponding tree in the left-hand branch. This isn't a problem: we just need to ensure that we nest it within the appropriate tree 12. There are two additional complications here. The first is that the justification contains a comma, so we need to surround the argument we give just with curly brackets. That is, we must write just={5,9 \$=\elim\$} or just={\$=\elim\$:{simple,!u}}. The second is that we wish to close this branch with an indication of the line numbers containing inconsistent *wffs*. We can use close={8,10} for this or we can use the same referencing system we used to reference lines when specifying justifications and write close={:to Pb or not to Pb,!c}. In either case, we again surrounding the argument with curly brackets to protect the comma. !c refers to the current line — something useful in many close annotations, but not helpful in specifying non-circular justifications.

```
\begin{tableau}
  {
    to prove={(\exists x)((\forall y)(Py \lif x = y) \land Px) \sststile{}{} (\exists x)(\forall y)(
Py  \lim x = y 
 7
  [(\operatorname{vxists} x)((\operatorname{vxist} y)(\operatorname{Py} \operatorname{if} x = y) \operatorname{Px})], checked=a, just=Pr., name=pr
    [{\lnot (\exists x)(\forall y)(Py \liff x = y)}, subs=a, just=Conc.~neg., name=neg conc
      [{(\forall y)(Py \lif a = y) \land Pa}, checked, just=$\exists\elim$:pr
         [{(\forall y)(Py \lif a = y)}, subs=b, just=$\land\elim$:!u, name=mark
           [Pa, just=$\land\elim$:!uu, name=simple
             [{\lnot (\forall y)(Py \liff a = y)}, checked=b, just=$\lnot\exists\elim$:neg conc
               [{\lnot (Pb \liff a = b)}, checked, just=$\lnot\forall\elim$:!u
                 [Pb, just=$\liff\elim$:!u, name=to Pb or not to Pb
                  [a \neq b, just=$\liff\elim$:!u
                  ٦
                 ٦
                 [\lnot Pb
                  [{a = b}]
                      [Pb, just={$=\elim$:{simple,!u}}, close={:to Pb or not to Pb,!c}
                     ٦
                  ]
                 ]
               ]
            ]
          ]
        ]
      ]
    ]
 ٦
\end{tableau}
```

This completes the main right-hand branch of the tree and we can focus solely on the remaining left-hand one. Tree 12 is straightforward — we just need to nest it within the left-hand tree 12.

```
\begin{tableau}
  {
    to prove={(\exists x)((\forall y)(Py \lif x = y) \land Px) \sststile{}{} (\exists x)(\forall y)(
    Py \liff x = y)}
    }
    [{(\exists x)((\forall y)(Py \lif x = y) \land Px)}, checked=a, just=Pr., name=pr
```

```
[{\lnot (\exists x)(\forall y)(Py \liff x = y)}, subs=a, just=Conc.~neg., name=neg conc
      [{(\forall y)(Py \lif a = y) \land Pa}, checked, just=$\exists\elim$:pr
        [{(\forall y)(Py \lif a = y)}, subs=b, just=$\land\elim$:!u, name=mark
          [Pa, just=$\land\elim$:!uu, name=simple
            [{\lnot (\forall y)(Py \liff a = y)}, checked=b, just=$\lnot\exists\elim$:neg conc
              [{\lnot (Pb \liff a = b)}, checked, just=$\lnot\forall\elim$:!u
                [Pb, just=$\liff\elim$:!u, name=to Pb or not to Pb
                 [a \neq b, just=$\liff\elim$:!u
                  [{Pb \lif a = b}, checked, just=$\forall\elim$:mark%, move by=1
                 1
                ]
                ٦
                [\lnot Pb
                 [{a = b}]
                    [Pb, just={$=\elim$:{simple,!u}}, close={:to Pb or not to Pb,!c}
                    ٦
                ٦
                ]
             ]
           ]
         ]
       1
     ]
   ]
 1
\end{tableau}
```

At this point, the main left-hand branch itself branches, so we have two trees 12. Treating this in the same way as the earlier branch at 12, we use two sets of square brackets nested within those for tree 12, but with neither nested within the other. Since we also want to mark the leftmost branch as closed, we add close={:to Pb or not to Pb,!c} in the same way as before.

```
\begin{tableau}
      {
           to prove={(|x| x = y| | x = 
Py  \lim x = y 
     }
      [{(xists x)((forall y)(Py lif x = y) land Px)}, checked=a, just=Pr., name=pr
            [{\lnot (\exists x)(\forall y)(Py \liff x = y)}, subs=a, just=Conc.~neg., name=neg conc
                   [{(\forall y)(Py \lif a = y) \land Pa}, checked, just=$\exists\elim$:pr
                         [{(\forall y)(Py \lif a = y)}, subs=b, just=$\land\elim$:!u, name=mark
                               [Pa, just=$\land\elim$:!uu, name=simple
                                     [{\lnot (\forall y)(Py \liff a = y)}, checked=b, just=$\lnot\exists\elim$:neg conc
                                           [{\lnot (Pb \liff a = b)}, checked, just=$\lnot\forall\elim$:!u
                                                  [Pb, just=$\liff\elim$:!u, name=to Pb or not to Pb
                                                     [a \neq b, just=$\liff\elim$:!u
                                                        [{Pb \lif a = b}, checked, just=4 $\forall\elim$
                                                                    [\lnot Pb, close={:to Pb or not to Pb,!c}, just=$\lif\elim$:!u
                                                                    1
                                                                    [{a = b}]
                                                                    ٦
                                                       ]
                                                 ]
                                                 ٦
                                                 [\lnot Pb
                                                    [{a = b}]
                                                              [Pb, just={$=\elim$:{simple,!u}}, close={:to Pb or not to Pb,!c}
                                                              ]
                                                    ]
                                                ]
                                           ]
```



We complete our initial specification by nesting 12 within the appropriate tree 12, again marking closure appropriately.

```
\begin{tableau}
 {
   to prove={(\exists x)((\forall y)(Py \lif x = y) \land Px) \sststile{}{} (\exists x)(\forall y)(
Py  \lim x = y 
 }
 [{(\exists x)((\forall y)(Py \lif x = y) \land Px)}, checked=a, just=Pr., name=pr
    [{\lnot (\exists x)(\forall y)(Py \liff x = y)}, subs=a, just=Conc.~neg., name=neg conc
      [{(\forall y)(Py \lif a = y) \land Pa}, checked, just=$\exists\elim$:pr
        [{(\forall y)(Py \lif a = y)}, subs=b, just=$\land\elim$:!u, name=mark
          [Pa, just=$\land\elim$:!uu, name=simple
            [{\lnot (\forall y)(Py \liff a = y)}, checked=b, just=$\lnot\exists\elim$:neg conc
              [{\lnot (Pb \liff a = b)}, checked, just=$\lnot\forall\elim$:!u
                [Pb, just=$\liff\elim$:!u, name=to Pb or not to Pb
                 [a \neq b, just=$\liff\elim$:!u
                  [{Pb \lif a = b}, checked, just=4 $\forall\elim$
                      [\lnot Pb, close={:to Pb or not to Pb,!c}, just=$\lif\elim$:!u
                      ]
                      [{a = b}]
                        [a \neq a, close={:!c}, just={$=\elim$:{!uuu,!u}}
                        ٦
                      ]
                  ]
                ]
                ]
                [\lnot Pb
                 [{a = b}]
                    [Pb, just={$=\elim$:{simple,!u}}, close={:to Pb or not to Pb,!c}
                    ٦
                 ٦
               ]
              ]
           ]
         ]
       ]
     ]
   ]
 ]
\end{tableau}
```

Compiling our code, we find that the line numbering is not quite right:

$(\exists x)((\forall y)(Py \to x = y) \land Px) \models (\exists x)(\forall y)(\forall y)(Py \to x = y) \land Px) \models (\exists x)(\forall y)(\forall y)(Py \to x = y) \land Px) \models (\exists x)(\forall y)(Py \to x = y) \land Px) \models (\exists x)(\forall y)(Py \to x = y) \land Px) \models (\exists x)(\forall y)(Py \to x = y) \land Px) \models (\exists x)(\forall y)(Py \to x = y) \land Px) \models (\exists x)(\forall y)(Py \to x = y) \land Px) \models (\exists x)(\forall y)(Py \to x = y) \land Px) \models (\forall x)(\forall y)(Py \to x = y) \land Px) \models (\forall x)(\forall y)(Py \to x = y) \land Px) \models (\forall x)(\forall y)(Py \to x = y) \land Px) \models (\forall x)(\forall y)(Py \to x = y) \land Px) \models (\forall x)(\forall y)(Py \to x = y) \land Px) \models (\forall x)(\forall y)(Py \to x = y) \land Px) \models (\forall x)(\forall y)(Py \to x = y) \land Px) \models (\forall x)(\forall y)(Py \to x = y) \land Px) \models (\forall x)(\forall y)(Py \to x = y) \land Px) \models (\forall x)(\forall y)(Py \to x = y) \land Px) \models (\forall x)(\forall y)(Py \to x = y) \land Px) \models (\forall x)(\forall y)(Py \to x = y) \land Px) \models (\forall x)(\forall x)(Py \to x = y) \land Px) \models (\forall x)(\forall x)(Py \to x = y) \land Px) \models (\forall x)(\forall x)(Py \to x = y) \land Px) \models (\forall x)(\forall x)(Py \to x = y) \land Px) \models (\forall x)(Py \to x) \land Px) \models (\forall x)(Py \to x) \land Px) \land Px) \models (\forall x)(Py \to x) \land Px) \models (\forall x)(Py \to x) \land Px) \models (\forall x)(Py \to x) \land Px) $	$(\forall y)(Py \leftrightarrow x = y)$
1. $(\exists x)((\forall y)(Py \rightarrow x = y) \land Px)$	√a Pr.
2. $\neg(\exists x)(\forall y)(Py \leftrightarrow x = y) \setminus a$	Conc. neg.
3. $(\forall y)(Py \rightarrow a = y) \land Pa \checkmark$	$1 \exists E$
4. $(\forall y)(Py \to a = y) \setminus b$	$3~\wedge\mathrm{E}$
5. Pa	$3~\wedge\mathrm{E}$
6. $\neg(\forall y)(Py \leftrightarrow a = y) \checkmark b$	$2 \neg \exists E$
7. $\neg (Pb \leftrightarrow a = b) \checkmark$	$6 \neg \forall E$
8. Pb $\neg Pb$	$7 \leftrightarrow \mathrm{E}$
9. $a \neq b$ $a = b$	$8 \leftrightarrow E$
10. $Pb \rightarrow a = b \checkmark Pb$	$4 \forall E; 5, 9 = E$
\sim \otimes	
11. $\neg Pb a = b$ ^{8,10}	$10 \rightarrow E$
12. $\otimes a \neq a$	9,11 = E
8,11	
12	
prooftroop warna ug about thig	

prooftrees warns us about this:

Package prooftrees Warning: Merging conflicting justifications for line 10! Please examine the output carefully and use "move by" to move lines later in the proof if required. Details of how to do this are included in the documentation.

We would like line 10 in the left-hand branch to be moved down by one line, so we add move by=1 to the relevant line of our proof. That is, we replace the line

[{Pb \lif a = b}, checked, just=4 \$\forall\elim\$

by

[{Pb \lif a = b}, checked, just=\$\forall\elim\$:mark, move by=1

giving us the following code:

```
\begin{tableau}
      {
            to prove={(|x| x = y| | x = 
Py  \lim x = y 
     }
      [{(xists x)((forall y)(Py lif x = y) land Px)}, checked=a, just=Pr., name=pr
             [{\lnot (\exists x)(\forall y)(Py \liff x = y)}, subs=a, just=Conc.~neg., name=neg conc
                   [{(\forall y)(Py \lif a = y) \land Pa}, checked, just=$\exists\elim$:pr
                         [{(\forall y)(Py \lif a = y)}, subs=b, just=$\land\elim$:!u, name=mark
                                [Pa, just=$\land\elim$:!uu, name=simple
                                      [{\lnot (\forall y)(Py \liff a = y)}, checked=b, just=$\lnot\exists\elim$:neg conc
                                            [{\lnot (Pb \liff a = b)}, checked, just=$\lnot\forall\elim$:!u
                                                   [Pb, just=$\liff\elim$:!u, name=to Pb or not to Pb
                                                      [a \neq b, just=$\liff\elim$:!u
                                                         [{Pb \lif a = b}, checked, just=$\forall\elim$:mark, move by=1
                                                                     [\lnot Pb, close={:to Pb or not to Pb,!c}, just=$\lif\elim$:!u
                                                                     1
                                                                     [{a = b}]
                                                                           [a \neq a, close={:!c}, just={$=\elim$:{!uuu,!u}}
                                                                           ]
                                                                     ]
                                                        ]
                                                 ]
                                                 ]
```



which produces our desired result:

$(\exists x)((\forall y)(Py \to x = y) \land Px) \vdash (\exists x)(\forall y)(Py \to x = y) \land Px) \models (\exists x)(\forall y)(Py \to x = y) \land Px) \models (\forall y)(\forall y)(Py \to x = y) \land Px) \models (\forall y)(\forall y)(Py \to x = y) \land Px) \models (\forall y)(\forall y)(Py \to x = y) \land Px) \models (\forall y)(\forall y)(Py \to x = y) \land Px) \models (\forall y)(\forall y)(Py \to x = y) \land Px) \models (\forall y)(\forall y)(\forall y)(\forall y)(\forall y)(\forall y)(\forall y)(\forall y$	$y \leftrightarrow x = y)$
1. $(\exists x)((\forall y)(Py \to x = y) \land Px) \checkmark a$	Pr.
2. $\neg(\exists x)(\forall y)(Py \leftrightarrow x = y) \setminus a$	Conc. neg.
3. $(\forall y)(Py \rightarrow a = y) \land Pa \checkmark$	$1 \exists E$
4. $(\forall y)(Py \to a = y) \setminus b$	$3 \wedge E$
5. Pa	$3 \wedge E$
$6. \qquad \neg(\forall y)(Py \leftrightarrow a = y) \checkmark b$	$2 \neg \exists E$
7. $\neg (Pb \leftrightarrow a = b) \checkmark$	$6 \neg \forall E$
8. $Pb \neg Pb$	$7 \leftrightarrow E$
9. $a \neq b$ $a = b$	$8 \leftrightarrow E$
10. <i>Pb</i>	5, 9 = E
11. $Pb \rightarrow a = b \checkmark \otimes$	$4 \forall E$
8,10	
12. $\neg Pb a = b$	$11 \rightarrow E$
13. $\otimes a \neq a$	9,12 = E
8,12 🛞	
13	

4 Loading the Package

To load the package simply add the following to your document's preamble.

\usepackage{prooftrees}

prooftrees will load forest automatically.

The only option currently supported is tableaux. If this option is specified, the prooftree environment will be called tableau instead.

Example: \usepackage[tableaux]prooftrees

would cause the tableau environment to be defined rather than prooftree.

Any other options given will be passed to forest.

Example: \usepackage[debug]prooftrees

would enable forest's debugging.

If one or more of forest's libraries are to be loaded, it is recommended that these be loaded separately and their defaults applied, if applicable, within a local T_EX group so that they do not interfere with prooftrees's environment.

5 Invocation

prooftree \l environment

The $\langle tree \ preamble \rangle$ is used to specify any non-default options which should be applied to the tree. It may contain any code valid in the preamble of a regular forest tree, in addition to setting prooftree options. The preamble may be empty, but the argument is *required*¹. The $\langle tree \ specification \rangle$ specifies the tree in the bracket notation parsed by forest.

Users of forest should note that the environments prooftree and forest differ in important ways.

- proof tree's argument is mandatory.
- The tree's preamble cannot be given in the body of the environment.
- \end{proof tree} must follow the (tree specification) immediately.

tableau $\begin{tableau}{\tree preamble}{\tree preamble}{\tree specification}\end{tableau} environment$

A substitute for prooftree, defined *instead* of prooftree if the package option tableaux is specified or a \prooftree macro is already defined when prooftrees is loaded. See section 4 for details and section 10 for this option's raison d'être.

6 Proof Tree Anatomy

The following diagram provides an overview of the configuration and anatomy of a prooftrees proof tree. Detailed documentation is provided in section 7 and section 8.

¹Failure to specify a required argument does not always yield a compilation error in the case of environments. However, failure to specify required arguments to environments often fails to achieve the best consequences, even when it does not result in compilation failures, and will, therefore, be avoided by the prudent.



7 Options

Most configuration uses the standard key/value interface provided by TikZ and extended by forest. These are divided into those which determine the overall appearance of the proof as a whole and those with more local effects.

7.1 Global Options

The following options affect the global style of the tree and should typically be set in the tree's preamble if non-default values are desired. The default values for the document can be set outside the prooftree environment using $forestset{settings}$. If only proof trees will be typeset, a default style can be configured using forest's default preamble.

auto move	= true false
not auto move	
Forest boolean register	Default: true

Determines whether **prooftrees** will move lines automatically, where possible, to avoid combining different justifications when different branches are treated differently. The default is to avoid conflicts automatically where possible. Turning this off permits finer-grained control of what gets moved using **move** by. The following are equivalent to the default setting:

auto move auto move=true

Either of the following will turn auto move off:

not auto move auto move=false

line numbering not line numbering Forest boolean register = true|false

Default: true

This determines whether lines should be numbered. The default is to number lines. The following are equivalent to the default setting:

line numbering line numbering=true

Either of the following will turn line numbering off:

not line numbering
line numbering=false

justifications not justifications Forest boolean register

= true|false

This determines whether justifications for lines of the proof should be typeset to the right of the tree. It is rarely necessary to set this option explicitly as it will be automatically enabled if required. The only exception concerns a proof for which a line should be moved but no justifications are specified. In this case either of the following should be used to activate the option:

justifications justifications=true

This is not necessary if just is used for any line of the proof.

single branches not single branches Forest boolean register = true|false

Default: false

This determines whether inference steps which do not result in at least two branches should draw and explicit branch. The default is to not draw single branches explicitly. The following are equivalent to the default setting:

not single branches
single branches=false

Either of the following will turn line numbering off:

single branches single branches=true

line no width Forest dimension register	= $\langle dimension \rangle$
	The maximum width of line numbers. By default, this is set to the width of the formatted line number 99.
	Example: line no width=20pt
just sep Forest dimension register	= $\langle dimension \rangle$
	Default: 1.5em
	Amount by which to shift justifications away from the tree. A larger value will shift the justifications further to the right, increasing their distance from the tree, while a smaller one will decrease this distance. Note that a negative value ought never be given. Although this will not cause an error, it may result in strange things happening. If you wish to decrease the distance between the tree and the justifications further, please set just sep to zero and use the options provided by forest and/or TikZ to make further negative adjustments.
	Example: just sep=.5em
line no sep Forest dimension register	= $\langle dimension \rangle$
	Default: 1.5em
	Amount by which to shift line numbers away from the tree. A larger value will shift the line numbers further to the left, increasing their distance from the tree, while a smaller one will decrease this distance. Note that a negative value ought never be given. Although this will not cause an error, it may result in strange things happening. If you wish to decrease the distance between the tree and the line numbers further, please set line no sep to zero and use the options provided by forest and/or TikZ to make further negative adjustments.
	Example: line no sep=5pt
close sep Forest dimension register	= $\langle dimension \rangle$
	Default: .75\baselineskip
	Distance between the symbol marking branch closure and any following annotation. If the format of such annotations is changed with close format, this dimension may require adjustment.
	Example: close sep=\baselineskip
proof tree inner proof	= $\langle dimension \rangle$
Width Forest dimension register	Default: Opt
proof tree inner proof	= $\langle dimension \rangle$
midpoint Forest dimension register	Default: Opt
line no shift Forest count register	= $\langle integer \rangle$
1 UI COL CULIEL I CHESTEL	Default: 0
	This value increments or decrements the number used for the first line of the proof. By default, line numbering starts at 1.
	Example: line no shift=3
	would begin numbering the lines at 4.
zero start	Start line numbering from 0 rather than 1. The following are equivalent:
Forest style	zero start line no shift=-1

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to prove Forest style	$=\langle wff \rangle$
	Statement of theorem or entailment to be typeset above the proof. In many cases, it will be necessary to enclose the statement in curly brackets.
	<pre>Example: to prove={{} P \lif P}</pre>
	By default, the content is expected to be suitable for typesetting in maths mode and should <i>not</i> , therefore, be enclosed by dollar signs or equivalent.
check with	= $\langle symbol \rangle$
Porest toks register	Default: $\operatorname{ensuremath}(\operatorname{checkmark}(\checkmark)$
	Symbol with which to mark discharged lines.
	Example: check with={\text{\ding{52}}}
	Within the tree, checked is used to identify discharged lines.
check right	= true false
not check right Forest boolean register	Default: true
	Determines whether the symbol indicating that a line is discharged should be placed to the right of the wff . The alternative is, unsurprisingly, to place it to the left of the wff . The following are equivalent to the default setting:
	check right check right=true
check left Forest style	Set check right=false. The following are equivalent ways to place the markers to the left:
	check right=false not check right check left
close with Forest toks register	= $\langle symbol \rangle$
-	Default: $\operatorname{ensuremath}\{\operatorname{otimes}\}$ (\otimes)
	Symbol with which to close branches.
	Example: close with={\ensuremath{\ast}}
	Within the tree, close is used to identify closed branches.
close with format	= $\langle key-value \ list \rangle$
Forest keylist register	Additional $TikZ$ keys to apply to the closure symbol. Empty by default.
	Example: close with format={red, font=}
	To replace a previously set value, rather than adding to it, use close with format' rather than close with format.
close format Forest keylist register	= $\langle key-value \ list \rangle$
	Default: font=\scriptsize
	Additional Ti kZ keys to apply to any annotation following closure of a branch.
	<pre>Example: close format={font=\footnotesize\sffamily, text=gray!75}</pre>
	To replace the default value of close format, rather than adding to it, use close format' rather than close format.

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	Example: close format'={text=red}
	will produce red annotations in the default font size, whereas
	Example: close format={text=red}
	will produce red annotations in \scriptsize.
subs with	= $\langle symbol \rangle$
Porest toks register	Default: $\operatorname{lash} (\)$
	Symbol to indicate variable substitution.
	Example: \text{:}
	Within the tree, subs is used to indicate variable substitution.
subs right	= true false
Forest boolean register	Default: true
	Determines whether variable substitution should be indicated to the right of the wff . The alternative is, again, to place it to the left of the wff . The following are equivalent to the default setting:
	subs right subs right=true
subs left Forest style	Set subs right=false. The following are equivalent ways to place the annotations to the left:
Forest style	subs right=false not subs right subs left
just refs left not just refs left	= true false
Forest boolean register	Default: true
	Determines whether line number references should be placed to the left of justifications. The alternative is to place them to the right of justifications. The following are equivalent to the default setting:
	just refs left just refs left=true
just refs right Forest style	Set just refs left=false. The following are equivalent ways to place the references to the right:
	just refs left=false not just refs left just refs right
	Note that this setting only affects the placement of line numbers specified using the cross-referencing system explained in section 7.2. Hard-coded line numbers in justifications will be typeset as is.
just format	= $\langle key-value \ list \rangle$
1 01 COL NCYLIOL TEYLOLET	Additional Ti kZ keys to apply to line justifications. Empty by default.
	Example: just format={red, font=}
	To replace a previously set value, rather than adding to it, use just format' rather than just format.

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line no format Forest keylist register	= $\langle key-value \ list \rangle$
	Additional $TikZ$ keys to apply to line numbers. Empty by default.
	Example: line no format={align=right, text=gray}
	To replace a previously set value, rather than adding to it, use line no format' rather than line no format. To change the way the number itself is formatted — to eliminate the dot, for example, or to put the number in brackets — redefine \linenumberstyle (see section 8).
wff format	= $\langle key-value \ list \rangle$
Forest keylist register	Additional $TikZ$ keys to apply to <i>wffs</i> . Empty by default.
	Example: wff format={draw=orange}
	To replace a previously set value, rather than adding to it, use wff format' rather than wff format.
proof statement format	= $\langle key-value \ list \rangle$
Forest keylist register	Additional $TikZ$ keys to apply to the proof statement. Empty by default.
	<pre>Example: proof statement format={text=gray, draw=gray}</pre>
	To replace a previously set value, rather than adding to it, use proof statement format' rather than proof statement format.
highlight format Forest autowrapped toks register	= $\langle key-value \ list \rangle$
	Default: draw=gray, rounded corners
	Additional $TikZ$ keys to apply to highlighted wffs.
	Example: highlight format={text=red}
	To apply highlighting, use the highlight wff, highlight just, highlight line no and/or highlight line keys (see section 7.2).
merge delimiter Forest toks register	= $\langle punctuation \rangle$
	Default: \text{; } (;)
	Punctuation to separate distinct justifications for a single proof line. Note that prooftrees will issue a warning if it detects different justifications for a single proof line and will suggest using move by to avoid the need for merging justifications. In general, justifications ought not be merged because it is then less clear to which $wff(s)$ each justification applies. Moreover, later references to the proof line will be similarly ambiguous. That is, merge delimiter ought almost never be necessary because it is almost always better to restructure the proof to avoid ambiguity.
	7.2 Local Options
	The following options affect the local structure or appearance of the tree and should typically be passed as options to the relevant node(s) within the tree.
grouped not grouped Forest boolean option	Indicate that a line is not an inference. When single branches is false, as it is with the default settings, this key is applied automatically and need not be given in the specification of the tree. When single branches is true, however, this key must be specified for any line which ought not be treated as an inference.
	Example: grouped
checked	Mark a complex wff as resolved, discharging the line.
Forest style	Example: checked
checked Forest style	= $\langle name \rangle$

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Existential elimination, discharge by substituting $\langle name \rangle$.

Example: checked=a

close Close branch.

Example: close = (annotation)

close Forest style

Forest style

= $\langle \text{annotation prefix} \rangle : \langle \text{references} \rangle$

Close branch with annotation. In the simplest case, $\langle annotation \rangle$ contains no colon and is typeset simply as it is. Any required references to other lines of the proof are assumed to be given explicitly.

Example: close={12,14}

If $\langle annotation \rangle$ includes a colon, prooftrees assumes that it is of the form $\langle annotation prefix \rangle$: $\langle references \rangle$. In this case, the material prior to the colon should include material to be typeset before the line numbers and the material following the colon should consist of one or more references to other lines in the proof. In typical cases, no prefix will be required so that the colon will be the first character. In case there is a prefix, prooftrees will insert a space prior to the line numbers. $\langle references \rangle$ may consist of either forest names (e.g. given by name= $\langle name \ label \rangle$) or forest relative node names (e.g. $\langle nodewalk \rangle$) or a mixture.

Example: close={:negated conclusion}

where name=negated conclusion was used to label an earlier proof line negated conclusion. If multiple references are given, they should be separated by commas and either $\langle references \rangle$ or the entire $\langle annotation \rangle$ must be enclosed in curly brackets, as is usual for TikZ and forest values containing commas.

Example: close={:!c,!uuu}

subs Forest style

Universal instantiation, instantiate with $\langle name \rangle$ or $\langle names \rangle$.

Example: subs={a,b}

just Forest autowrapped toks option = $\langle justification \rangle$

= $\langle name \rangle / \langle names \rangle$

= (justification prefix/suffix):(references)

Justification for inference. This is typeset in text mode. Hence, mathematical expressions must be enclosed suitably in dollar signs or equivalent. In the simplest case, $\langle justification \rangle$ contains no colon and is typeset simply as it is. Any required references to other lines of the proof are assumed to be given explicitly.

Example: just=3 \$\lor\$D

If $\langle justification \rangle$ includes a colon, prooftrees assumes that it is of the form $\langle justification prefix/suffix \rangle$: $\langle references \rangle$. In this case, the material prior to the colon should include material to be typeset before or after the line numbers and the material following the colon should consist of one or more references to other lines in the proof. Whether the material prior to the colon is interpreted as a $\langle justification prefix \rangle$ or a $\langle justification suffix \rangle$ depends on the value of just refs left. $\langle references \rangle$ may consist of either forest names (e.g. given by name= $\langle name label \rangle$ and then used as $\langle name label \rangle$) or forest relative node names (e.g. $\langle nodewalk \rangle$) or a mixture. If multiple references are given, they should be separated by commas and $\langle references \rangle$ must be enclosed in curly brackets. If just refs left is true, as it is by default, then the appropriate line number(s) will be typeset before the $\langle justification suffix \rangle$.

Example: just=\$\lnot\exists\$\elim:{!uu,!u}

If just refs left is false, then the appropriate line number(s) will be typeset after the $\langle justification \ prefix \rangle$.

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Example: just=From:bertha

= $\langle positive integer \rangle$ move by

Forest style

Move the content of the current line $\langle positive integer \rangle$ lines later in the proof. If the current line has a justification and the content is moved, the justification will be moved with the line. Later lines in the same branch will be moved appropriately, along with their justifications.

Example: move by=3

Note that, in many cases, prooftrees will automatically move lines later in the proof. It does this when it detects a condition in which it expects conflicting justifications may be required for a line while initially parsing the tree. Essentially, **prooftrees** tries to detect cases in which a branch is followed closely by asymmetry in the structure of the branches. This happens, for example, when the first branch's first wff is followed by a single wff, while the second branch's first wff is followed by another branch. Diagrammatically:



In this case, **prooftrees** tries to adjust the tree by moving lines appropriately if required.

However, this detection is merely structural — prooftrees does not examine the content of the wffs or justifications for this purpose. Nor does it look for slightly more distant structural asymmetries, conflicting justifications in the absence of structural asymmetry or potential conflicts with justifications for lines in other, more distant parallel branches. Although it is not that difficult to detect the *need* to move lines in a greater proportion of cases, the problem lies in providing general rules for deciding how to resolve such conflicts. (Indeed, some such conflicts might be better left unresolved e.g. to fit a proof on a single Beamer slide.) In these cases, a human must tell **prooftrees** if something should be moved, what should be moved and how far it should be moved.

Because simple cases are automatically detected, it is best to typeset the proof before deciding whether or where to use this option since **prooftrees** will assume that this option specifies movements which are required *in addition to* those it automatically detects. Attempting to move a line 'too far' is not advisable. proof trees tries to simply ignore such instructions, but the results are likely to be unpredictable.

Not moving a line far enough — or failing to move a line at all — may result in the content of one justification being combined with that of another. This happens if just is specified more than once for the same proof line with differing content. prooftrees does examine the content of justifications for this purpose. When conflicting justifications are detected for the same proof line, the justifications are merged and a warning issued suggesting the use of move by.

highlight wff not hightlight wff Forest boolean option

highlight just not hightlight just Forest boolean option Example: highlight wff

Highlight wff.

Highlight justification.

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	Example: highlight just
highlight line no not highlight line no Forest boolean option	Highlight line number.
	Example: highlight line no
highlight line	Highlight proof line.
not highlight line Forest boolean option	Example: highlight line
line no options	= $\langle key-value \ list \rangle$
Forest autowrapped toks option	Additional $TikZ$ keys to apply to the line number for this line.
	Example: line no options={blue}
just options	= $\langle key-value \ list \rangle$
Forest autowrapped toks option	Additional $TikZ$ keys to apply to the justification for this line.
	Example: just options={draw, font=\bfseries}
wff options	= $\langle key-value \ list \rangle$
Forest autowrapped toks option	Additional $TikZ$ keys to apply to the <i>wff</i> for this line.
	Example: wff options={magenta, draw}
	Note that this key is provided primarily for symmetry as it is faster to simply give the options directly to forest to pass on to $TikZ$. Unless wff format is set to a non-default value, the following are equivalent:
	wff options={magenta, draw} magenta, draw
line options	= $\langle key-value \ list \rangle$
Forest autowrapped toks option	Additional $TikZ$ keys to apply to this proof line.
	Example: line options={draw, rounded corners}
line no override	= $\langle text \rangle$
Forest style	Substitute $\langle text \rangle$ for the programmatically-assigned line number. $\langle text \rangle$ will be wrapped by \linenumberstyle , so should not be anything which would not make sense in that context.
	Example: line no override={n}
no line no	
Forest style	Do not typeset a line number for this line. Intended for use in trees where line numbering is activated, but some particular line should not have its number typeset. Note that the number for the line is still assigned and the node which would otherwise contain that number is still typeset. If the next line is automatically numbered, the line numbering will, therefore, 'jump', skipping the omitted number.
	Example: no line no

8 Macros

 $\linenumberstyle {\langle number \rangle}$

macro

This macro is responsible for formatting the line numbers. The default definition is

```
\newcommand*\linenumberstyle[1]{#1.}
```

It may be redefined with **\renewcommand*** in the usual way. For example, if for some reason you would like bold line numbers, try

\renewcommand*\linenumberstyle[1]{\textbf{#1.}}

9 Memoization

Tableaux created by prooftrees cannot, in general, be externalised with TikZ's external library. Since pgf/TikZ, in general, and prooftrees, in particular, can be rather slow to compile, this is a serious issue. If you only have a two or three small tableaux, the compilation time will be negligible. But if you have large, complex proofs or many smaller ones, compilation time will quickly become excessive.

Version 0.9 does not cure the disease, but it does offer an extremely effective remedy for the condition. While it does not make prooftrees any faster, it supports the memoize package developed by forest's author, Sašo Živanović (2023). Memoization is faster, more secure, more robust and easier to use than TikZ's externalisation.

- It is faster. It does not require separate compilations for each memoized object, so it is comparatively fast even when memoizing.
- It is more secure. It requires only restricted shell-escape, which almost all T_EX installations enable by default, so it is considerably more secure and can be utilised even where shell-escape is disabled.
- It is more robust. It can successfully memoize code which defeats all ordinary mortals' attempts to externalize with the older TikZ library.
- It is easier to use. It requires less configuration and less intervention. For example, it detects problematic code and aborts memoization automatically in many cases in which TikZ's external would either cause a compilation error or silently produce nonsense output, forcing the user to manually disable the process for relevant code.

There is always a 'but', but this is a pretty small 'but' as 'but's go.

But installation requires slightly more work. To reap the full benefits, you want to use either the perl or the python 'extraction' method. There is a third method, which does not require any special installation, but this lacks several of the advantages explained above and is not recommended.

If you use T_EX Live, you have perl already, but you may need to install a couple of libraries. python is not a prerequisite for T_EX Live but, if you happen to have it installed, you will probably only need an additional library to use this method.

See Memoize (Živanović 2023) for further details.

Once you have the prerequisites setup, all you need do is load memoize before prooftrees.

```
\usepackage[extraction method=perl]{memoize}% or python
\usepackage{prooftrees}
```

After a single compilation, your document will have expanded to include extra pages. At this point, it will look pretty weird. After the next compilation, your document will return to its normal self, the only difference being the speed with which it does so as all your memoized tableaux will simply be included, as opposed to recompiled. Only when you alter the code for a tableau, delete the generated files, disable memoization or explicitly request it will the proof be recompiled.

Memoization is compatible with both prooftrees's cross-referencing system and $\text{IAT}_{\text{E}}X 2_{\varepsilon}$'s cross-references, but the latter require an additional compilation. In general, if a document element takes n compilations to stabilise, it will take n + 1 compilations to complete the memoization process. See *Memoize* (Živanović 2023) for details.

10 Compatibility

Versions of prooftrees prior to 0.5 are incompatible with bussproofs, which also defines a prooftree environment. Version 0.6 is compatible with bussproofs provided

either bussproofs is loaded before prooftrees

or prooffrees is loaded with option tableaux (see section 4).

In either case, prooftrees will *not* define a prooftree environment, but will instead define tableau. This allows you to use tableau for prooftrees trees and prooftree for bussproofs trees.

11 Version History

11.1 0.9

Add support for memoize and utilise for documentation.

Use \NewDocumentEnvironment, removing direct dependency on environ.

11.2 0.8

Add previously unnoticed dependency on $\mathsf{amstext}$. Attempt to fix straying closure symbols evident in documentation and a T_EX SE question²

Documentation now loads enumitem, since it depended on it already anyway and specifies doc2 in options for ltxdoc as the code is incompatible with the current version.

11.3 0.7

Implement auto move. See section 7.1. The main point of this option is to allow automatic moves to be switched off if one teaches students to first apply all available non-branching rules for the tableau as a whole, as opposed to all non-branching rules for the sub-tree. The automatic algorithm is consistent with the latter, but not former, approach. The algorithm favours compact trees, which are more likely to fit on beamer slides. Switching the algorithm off permits users to specify exactly how things should or should not be moved. Thanks to Peter Smith for prompting this.

Fix bug reported at tex.stackexchange.com/q/479263/39222.

11.4 0.6

Add compatibility option for use with **bussproofs**. See section 4. Thanks to Peter Smith for suggesting this.

$11.5 \quad 0.5$

Significant re-implementation leveraging the new argument processing facilities in forest 2.1. This significantly improves performance as the code is executed much faster than the previous pgfmath implementation.

11.6 0.41

Update for compatibility with forest 2.1.

²https://tex.stackexchange.com/q/619314/.

11.7 0.4

Bug fix release:

- line no shift was broken;
- in some cases, an edge was drawn where no edge belonged.

11.8 0.3

First CTAN release.

References

Hodges, Wilfred (1991). Logic: An Introduction to Elementary Logic. Penguin.

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A Implementation

```
1 %% Copyright 2016-2024 Clea F. Rees
2 %%
3 %% This work may be distributed and/or modified under the
4 %% conditions of the LaTeX Project Public License, either version 1.3c
_5 %% of this license or (at your option) any later version.
6 %% The latest version of this license is in
7 %%
     https://www.latex-project.org/lppl.txt
_{\rm 8} %% and version 1.3c or later is part of all distributions of LaTeX
9 %% version 2008-05-04 or later.
10 %%
11 %% This work has the LPPL maintenance status `maintained'.
12 %%
13 %% The Current Maintainer of this work is Clea F. Rees.
14 %%
15 %% This file may only be distributed together with a copy of the package
16 %% prooftrees.
17 %%
18 %% This work consists of all files listed in manifest.txt.
19 %%
21 \NeedsTeXFormat{LaTeX2e}
22 \RequirePackage{svn-prov}
23 \ProvidesPackageSVN{$Id: prooftrees.sty 10522 2024-10-23 16:31:08Z cfrees $}[v0.9 \revinfo]
_{24} % define \prooftrees@enw to hold the name of the environment
25 % default is to name the environment prooftree, this ensures backwards compatibility
26 \newcommand*\prooftrees@enw{prooftree}
_{\rm 27} % allow users to change the name to tableau using tableaux
28 \DeclareOption{tableaux}{\renewcommand*\prooftrees@enw{tableau}}
29 % just in case
30 \DeclareOption{tableau}{\renewcommand*\prooftrees@enw{tableau}}
31 \DeclareOption*{\PassOptionsToPackage{\CurrentOption}{forest}}
32 % if \prooftree is not yet defined, set the name to prooftree; otherwise, use tableau to avoid
  conflict with bussproofs (which uses 'prooftree' rather than 'bussproof' as one might expect)
33 \ifcsname prooftree\endcsname
    \renewcommand*\prooftrees@enw{tableau}%
34
35 \else
    \renewcommand*\prooftrees@enw{prooftree}%
36
37 \fi
38 % \ifundef\prooftree{\renewcommand*\prooftrees@enw{prooftree}}{\renewcommand*\prooftrees@enw{tableau
  }}
39 % let users override the default prooftree in case they need to load bussproofs later
40 \ProcessOptions
41 \RequirePackage{forest}[2016/12/04]
42 \RequirePackage{amssymb,amstext}
43 \newcommand*\linenumberstyle[1]{#1.}
44 % currently, keys starting 'proof tree' and macros starting 'prooftree' or 'prooftree@' are intended
  for internal use only
_{\rm 45} % this does not apply to the environment prooftree
_{46} % other keys and macros are intended for use in documents
47 % in particular, the style 'proof tree' is **NOT** intended to be used directly by the user and its
  direct use is **ABSOLUTELY NOT SUPPORTED IN ANY WAY, SHAPE OR FORM**; it is intended only for
  implicit use when the prooftree environment calls it
48 \forestset{% don't use @ in register/option names - the documentation is lying when it says non-
  alphanumerics will be converted to underscores when forming pgfmath functions ;)
```

- declare boolean register={line numbering},% line numbers
- line numbering,% default is for line numbers
 declare boolean register={justifications},% line justifications
- not justifications, % default is for no line justifications (b/c there's no point in enabling this if the user doesn't specify any content)

```
declare boolean register={single branches},% single branches: explicitly drawn branches and a
   normal level distance between lone children and their parents
     not single branches,% default is for lone children to be grouped with their parents
54
     declare boolean register={auto move},% ble mae'n bosibl, symud pethau'n awtomatig
     auto move, % default: symud yn awtomatig
56
     declare dimen register={line no width},% default will be set to the width of 99 wrapped in the line
57
    numbering style
     line no width'=Opt,% fallback default is Opt
58
     declare dimen register={just sep},% amount by which to shift justifications away from the main tree
59
     just sep'=1.5em,% default is 1.5em
60
     declare dimen register={just dist},% distance of justifications from centre of inner tree;
   overrides just sep
     just dist'=0pt,
62
     declare dimen register={line no sep},% amount by which to shift line numbers away from the main
63
   tree
     line no sep'=1.5em,
64
     declare dimen register={line no dist},% distance of line nos. from centre of inner tree; overrides
65
   line no sep
     line no dist'=0pt,
66
     declare dimen register={close sep},% distance between closure symbols and any following annotation
67
     close sep'=.75\baselineskip,
68
     declare dimen register={proof tree line no x},
69
     proof tree line no x'=Opt,
70
     declare dimen register={proof tree justification x},
71
     proof tree justification x'=Opt,
72
     declare dimen register={proof tree inner proof width},
73
     proof tree inner proof width'=Opt,
74
     declare dimen register={proof tree inner proof midpoint},
75
     proof tree inner proof midpoint'=Opt,
76
     declare count register={proof tree rhif lefelau},% count the levels in the proof tree
77
     proof tree rhif lefelau'=0,
78
     declare count register={proof tree lcount},% count the line numbers (on the left)
79
80
     proof tree lcount'=0,
     declare count register={proof tree jcount},% count the justifications (on the right)
81
82
     proof tree jcount'=0,
     declare count register={line no shift},% adjustment for line numbering
83
     line no shift'=0,
84
     declare count register={proof tree aros},
85
     proof tree aros'=0,
86
     declare toks register={check with},
87
     check with={\ensuremath{\checkmark}},
88
     declare boolean register={check right},
89
     check right,
90
     check left/.style={not check right},
91
     declare toks register={subs with},
92
     subs with={\ensuremath{\backslash}},
93
     declare boolean register={subs right},
94
     subs right,
95
     subs left/.style={not subs right},
96
     declare toks register={close with},
97
     close with={\ensuremath{\otimes}},
98
     declare keylist register={close format},
99
     close format={font=\scriptsize},
     declare keylist register={close with format},
     close with format={},
102
     declare toks register={merge delimiter},
103
     merge delimiter={\text{; }},
104
     declare boolean register={just refs left},
     just refs left.
106
     just refs right/.style={not just refs left},
107
```

```
108 declare keylist register={just format},
```

```
just format={},
     declare keylist register={line no format},
     line no format={},
     declare autowrapped toks register={highlight format},
     highlight format={draw=gray, rounded corners},
     declare keylist register={proof statement format},
114
     proof statement format={},
     declare keylist register={wff format},
116
     wff format={}.
117
     declare boolean={proof tree justification}{0},
118
     declare boolean={proof tree line number}{0},
119
     declare boolean={grouped}{0},
     declare boolean={proof tree phantom}{0},
     declare boolean={highlight wff}{0},
     declare boolean={highlight just}{0},
     declare boolean={highlight line no}{0},
124
     declare boolean={highlight line}{0},
125
     Autoforward={highlight line}{highlight just, highlight wff, highlight line no},
126
     declare boolean={proof tree toing}{0},
     declare boolean={proof tree toing with}{0},
128
     declare boolean={proof tree rhiant cymysg}{0},
129
     declare boolean={proof tree rhifo}{1},
130
     declare boolean={proof tree arweinydd}{0},
131
     declare autowrapped toks={just}{},
132
     declare toks={proof tree rhestr rhifau llinellau}{},
133
     declare toks={proof tree close}{},
134
     declare toks={proof tree rhestr rhifau llinellau cau}{},
     declare autowrapped toks={just options}{},
136
     declare autowrapped toks={line no options}{},
     declare autowrapped toks={wff options}{},
138
     declare autowrapped toks={line options}{},
139
     Autoforward={line options}{just options={#1}, line no options={#1}, wff options={#1}},
140
141
     declare count={proof tree toing by}{0},
     declare count={proof tree cadw toing by}{0},
     declare count={proof tree toooing}{0},
143
     declare count={proof tree proof line no}{0},
144
     % keylists for internal storage
145
     declare keylist={proof tree jrefs}{},
146
     declare keylist={proof tree crefs}{},
     % keylists for use in stages
148
     declare keylist={proof tree ffurf}{},
149
     declare keylist={proof tree symud awto}{},
     declare keylist={proof tree creu nodiadau}{},
     declare keylist={proof tree nodiadau}{},
     % > not documented yet, I think
     \% > now indicates use of process when it is the first token, preceding a list of instructions as
154
   opposed to pgfmath stuff
     define long step={proof tree symud}{}{%
       root,sort by={>{0}{level},>{_0<}{1}{n children}},sort'=descendants</pre>
156
     }.
     define long step={proof tree cywiro symud}{}{%
158
       root, if line numbering={n=2}{n=1}, sort by={>{0}{level},>{_0<}{1}{n children}, sort '=descendants
159
160
     }.
161
     define long step={proof tree camau}{}{% updated version of defn. from saso's code (forest2-saso-
   ptsz.tex) & http://chat.stackexchange.com/transcript/message/28321501#28321501
       root,sort by={>{0}{y},>{0w1+d}{x}{-##1}},sort'={filter={descendants}{>{00!&}{proof tree rhifo}{
162
   proof tree phantom}}}% angen +d - gweler http://chat.stackexchange.com/transcript/message
   /28607212#28607212
     Ъ.
163
     define long step={proof tree wffs}{}{% coeden brif yn unig ar ôl i greu nodiadau
164
       fake=root, if line numbering={n=2}{n=1}, tree
165
```

```
Ъ.
166
     checked/.style={% mark discharge with optional name substituted into existential
167
       delay={%
168
         if check right={%
169
            content+'={\ \forestregister{check with}#1},
         }{%
            +content'={\forestregister{check with}#1\ },
         },
       },
174
     },
     subs/.style={% mark substitution of name into universal
       delay={%
177
         if subs right={%
178
            content+'={\ \forestregister{subs with}#1},
         74%
180
            +content'={\forestregister{subs with}#1\ },
181
         },
182
       },
183
     },
184
     close/.style={% this now uses nodes rather than a label to accommodate annotations; closing must be
185
    done before packing the tree to ensure that sufficient space is allowed for the symbol and any
   following annotation; the annotations must be processed before anything is moved to ensure that the
   correct line numbers are used later, even if the references are given as relative node names
       if={%
186
         >{__=}{#1}{}%
187
       }{}{%
188
         temptoksb={},
189
         temptoksa={#1},
190
         split register={temptoksa}{:}{proof tree close,temptoksb},
         if temptoksb={}{}{%
            split register={temptoksb}{,}{proof tree cref},
         },
194
       },
       delay={%
         append={% this node holds the closure symbol
            [\forestregister{close with},
198
             not proof tree rhifo,
199
             proof tree phantom,
200
             grouped,
201
             no edge,
202
             process keylist register=close with format,
203
              before computing xy={% adjust the distance between the closure symbol and any annotation
204
                delay={%
205
                  l'=\baselineskip,% cywiro? fel arall, bydda'r peth byth yn cael ei wneud achos proof
206
   tree phantom? dim yn siwr o gwbl
207
                  for children={%
                    l/.register=close sep,
208
                  }.
209
                },
210
              },
211
              before drawing tree={%
212
                if={>{RR|}{line numbering}{justifications}}{%
213
                  proof tree proof line no/.option=!parent.proof tree proof line no,
214
                }{},
             },
216
              if={%
                >{__=}{#1}{}%
218
              }{}{% don't create a second node if there's no annotation
219
                delav={%
220
                  append={% this node holds the annotation, possibly including cross-references which
221
   will be relative to the node's grandparent
```

```
[,
222
                      not proof tree rhifo,
223
                      proof tree phantom,
224
                      grouped,
                      no edge,
                      process keylist register=close format,
227
                      if={%
228
                        >{0_=}{!parent,parent.proof tree close}{}%
                      }{}{content/.option=!{parent,parent}.proof tree close},
230
                      proof tree crefs/.option=!{parent,parent}.proof tree crefs,
                      delay={%
                        !{parent,parent}.proof tree crefs'={},
                      },
                      before drawing tree={%
                        if={>{RR|}{line numbering}{justifications}}{%
                          proof tree proof line no/.option=!{parent,parent}.proof tree proof line no,
                        }{},
238
                      },
                   ]%
240
                 },
241
               },
242
             },
243
           1%
244
         },
       },
246
     }.
     proof tree line no/.style={% creates the line numbers on the left; note that it *does* matter that
248
   these are part of the tree, even though they do not need to be packed or to have xy computed;
   moreover, it matters that each is the child of the previous line number... so it won't do for them to
    *remain* siblings, even though that's fine when they are created.
249
       anchor=base west,
       no edge,
250
       proof tree line number,
252
       text width/.register=line no width,
       x'/.register=proof tree line no x,
       process keylist register=line no format,
254
       delay={%
255
         proof tree lcount'+=1,
256
         tempcounta/.process={RRw2+n}{proof tree lcount}{line no shift}{##1+##2},
         content/.process={Rw1}{tempcounta}{\linenumberstyle{##1}},% content i.e. the line number
258
         name/.expanded={line no \foresteregister{tempcounta}},% name them so they can be moved later
259
         typeset node,
260
         if proof tree lcount>=3{% the initial location of most line numbers is incorrect and they must
261
   be moved
           for previous={% move the line number below the previous line number
262
263
              append/.expanded={line no \foresteregister{tempcounta}}
           }.
264
         }{},
265
       }.
266
     Ъ.
267
     proof tree line justification/.style={% creates the justifications on the right but does not yet
268
   specify any content
       anchor=base west,
269
       no edge,
270
       proof tree justification,
       x'/.register=proof tree justification x,
       process keylist register=just format,
273
       delay={%
274
         proof tree jcount'+=1,
275
         tempcounta/.process={RRw2+n}{proof tree jcount}{line no shift}{##1+##2},
276
         name/.expanded={just \foresteregister{tempcounta}},% name them so they can be moved
277
```

```
typeset node, % angen i osgoi broblemau 'da highlight just/line etc.
278
         if proof tree jcount>=3{% correct the location as for the line numbers (cf. line no style)
279
            for previous={%
280
              append/.expanded={just \foresteregister{tempcounta}},
281
            },
282
         }{},
283
       },
284
     },
285
     zero start/.style={%
286
       line no shift'+=-1,
287
     },
288
     to prove/.style={% sets a proof statement
289
       for root={%
290
         before typesetting nodes={%
291
            content={#1},
292
            phantom=false,
293
            baseline,
294
            if line numbering={anchor=base west}{anchor=base},
295
           process keylist register=proof statement format
         },
297
         before computing xy={%
298
            delay={%
299
              for children={%
300
                l=1.5*\baselineskip,
301
              }.
302
            },
303
         },
304
       },
305
     Ъ.
306
     proof tree/.style={% this style should **NOT** be used directly in a forest environment - see notes
307
    at top of this file
       for tree={%
308
         parent anchor=children,% manual 64
309
310
         child anchor=parent,% manual 64
         math content,
311
         delay={%
312
            if just={}{}{% if we've got justifications, make sure nodes are created for them later and
313
   split out cross-references so we identify the correct nodes before anything gets moved, allowing the
   use of relative node names
              justifications,
314
              temptoksa={},
315
              split option={just}{:}{just,temptoksa},
              if temptoksa={}{}{%
317
318
                split register={temptoksa}{,}{proof tree jref},
319
              },
            },
320
            if content={}{% if there's no proof statement
321
              if level=0{}{%
                shape=coordinate,
              }.
            }{},
         },
       },
327
       where level=0{%
328
         for children={% no edges from phantom root or proof statement to children
            before typesetting nodes={%
330
              no edge,
331
           },
332
         },
         delay={%
334
            if content={}{phantom}{},
335
```

```
if line numbering={% create the line numbers if appropriate
             parent anchor=south west,
337
              if line no width={0pt}{%
338
                line no width/.pgfmath={width("\noexpand\linenumberstyle{99}")},
339
              }{},
340
           }{}.
341
         },
342
         proof tree creu nodiadau={% this is processed after computing xy
            if={>{RR|}{line numbering}{justifications}}{% count proof lines if necessary
344
              proof tree rhif lefelau'/.register=line no shift,
              for proof tree camau={%
346
                if level>=1{%
347
                  if={%
3/18
                    >{00<}{y}{!back.y}%
349
                  74%
350
                    proof tree rhif lefelau'+=1,
351
                    proof tree proof line no'/.register=proof tree rhif lefelau,
352
                  }{%
                    proof tree proof line no'/.register=proof tree rhif lefelau
354
                  },
355
                }{},
356
             },
357
             proof tree inner proof midpoint/.min={>{00w2+d}{x}{min x}{##1+##2}}{fake=root,descendants},
358
             proof tree inner proof width/.max={>{00w2+d}{x}{max x}{##1+##2}}{fake=root,descendants},
359
             proof tree inner proof width-/.register=proof tree inner proof midpoint,
360
             proof tree inner proof midpoint+/.process={Rw+d{proof tree inner proof width}{##1/2}},
361
            }{},
362
            if line numbering={% get the x position of line numbers and adjust the location and alignment
363
    of the proof statement
             proof tree line no x/.min={>{00w2+d}{x}{min x}{##1+##2}}{fake=root,descendants},
364
              if={%
365
                > Rd= {line no dist}{0pt}%
366
              }{%
367
368
                proof tree line no x-/.register=line no sep,
              }{%
369
                tempdima/.register=proof tree inner proof width,
                tempdima:=2,
                if={%
372
                  > RR< {line no dist}{tempdima}%
373
                }{}{%
374
                  proof tree line no x/.register=proof tree inner proof midpoint,
375
                  proof tree line no x-/.register=line no dist,
376
                },
377
             },
378
             proof tree line no x-/.register=line no width,
379
380
              for root={%
                tempdimc/.option=x,
381
                x'+/.register=proof tree line no x,
382
                x'-/.option=min x,
383
              },
384
             prepend={% create line numbers on left
385
                [,
386
                  proof tree line no,
387
                  \% () to group are required here - otherwise, the -1 (or -2 or whatever) is silently
   ignored
                  repeat={((proof_tree_rhif_lefelau)-1)-(line_no_shift)}{% most are created in the wrong
389
   place but proof tree line no moves them later
                    delay n={proof_tree_lcount}{
390
                      append={[, proof tree line no]},
391
                    },
                  },
393
```

```
1%
394
             },
395
           }{},
396
            if justifications={% get the x position of justifications and create the nodes which will
397
   hold the justification content, if required
              proof tree justification x/.max={>{00w2+d}{x}{max x}{##1+##2}}{fake=root,descendants},
              if={%
                > Rd= {just dist}{0pt}%
400
              }{%
401
                proof tree justification x+/.register=just sep,
402
              }{%
403
                tempdima/.register=proof tree inner proof width,
404
                tempdima:=2,
405
                if={%
406
                  > RR< {just dist}{tempdima}%
407
                }{}{%
408
                  proof tree justification x/.register=proof tree inner proof midpoint,
409
                  proof tree justification x+/.register=just dist,
410
                },
411
              },
412
              append={%
                [,
414
415
                  proof tree line justification,
                  repeat={((proof_tree_rhif_lefelau)-1)-(line_no_shift)}{% most are created in the wrong
   place but proof tree line justification moves them later
                    delay n={proof_tree_jcount}{%
417
                      append={[, proof tree line justification]},
418
                    },
419
                  }%
420
                1%
421
              },
           }{},
423
         },
424
       }{%
         delay={%
426
           if single branches={}{% automatically group lines if not using single branches
427
              if n children=1{%
428
                for children={%
429
                  grouped,
430
                },
431
              }{},
432
           },
433
         },
434
         before typesetting nodes={% apply wff-specific highlighting and additional TikZ keys
435
           process keylist register=wff format,
436
437
            if highlight wff={node options/.register=highlight format}{},
           node options/.option=wff options,
438
         }.
439
       Ъ.
440
       proof tree ffurf={% processed before proof tree symud auto: adjusts the alignment of lines when
441
   some levels of the tree are grouped together either whenever the number of children is only 1 or by
   applying the grouped style to particular nodes when specifying the tree
         if auto move={%
442
            if single branches={%
443
              where={%
444
                >{0! _0< 0 &&}{grouped}{2}{level}{proof tree rhifo}%
445
              }{%
446
                if={%
447
                  >{_O= _O< &}{1}{!parent.n children}{1}{!parent,parent.n children}%
448
                }{%
449
                  not tempboola,
450
```

```
for root/.process={Ow1}{level}{%
451
                    for level={##1}{\%}
452
                      if={%
                        >{_0< _0= &}{1}{!parent.n children}{1}{n}%
454
                      7.4%
455
                        tempboola,
456
                      }{}.
457
                    }.
458
                  },
                  if tempboola={%
                    proof tree toing,
461
                  }{},
462
               }{},
463
             }{},
464
           }{},
465
           where={%
466
             >{0 _0< 0 &&}{grouped}{1}{level}{proof tree rhifo}%
467
           }{% this searches for certain kinds of structural asymmetry in the tree and attempts to move
468
   lines appropriately in such cases - the algorithm is intended to be relatively conservative (not in
   the sense of 'cautious' or 'safe' but in the sense of 'reflection of the overlapping consensus of
   reasonable users' / 'what would be rationally agreed behind the prooftrees veil of ignorance';
   however, I should have realised I actually had 'the overlapping concensus of reasonable Beamer users'
    in mind rather than 'the overlapping consensus of reasonable users', so there is now an option to
   turn it off; apologies if this comment previously misclassified you as 'unreasonable'; apologies for
   the inconvenience if you are an unreasonable user)
             not tempboola,
469
             for root/.process={Ow1}{level}{%
470
               for level={##1}{%
471
                  if={%
472
                    >{_0< _0= &}{1}{!parent.n children}{1}{n}%
473
                  }{%
474
                    tempboola,
475
476
                  }{},
               },
             },% Sao: http://chat.stackexchange.com/transcript/message/27874731#27874731, see also http
478
   ://chat.stackexchange.com/transcript/message/27874722#27874722
             if tempboola={%
479
               if n children=0{%
480
                  if={>{00|}{!parent.proof tree toing}{!parent.proof tree toing with}}{% we're already
481
   moving the parent and the child will move with the parent, so we can just mark this and do nothing
   else
                    proof tree toing with,
482
                  }{%
483
                    for root/.process={0w1}{level}{% don't move a terminal node even in case of asymmetry
484
   : instead, create a separate proof line for terminal nodes on this level which are only children, by
   moving children with siblings on this level down a proof line, without altering their physical
   location
                      % this makes the tree more compact and stops it looking silly
485
                      for level={##1}{%
486
                        if={%
487
                          >{_0< _0= &}{1}{!parent.n children}{1}{n}%
488
                        }{% this just serves to keep the levels nice for the sub-tree and ensure things
489
   align. We need this because we want to skip a level here to allow room for the terminal node in the
   other branch
                          for parent={%
490
                            if proof tree rhiant cymysg={}{% we mark the parent to avoid increasing the
   line number of its descendants more than once
                              proof tree rhiant cymysg,
492
                              for descendants={%
493
                                proof tree toing by '+=1,
494
                              },
495
```

```
},
496
                          },
497
                       }{},
498
                     },
499
                   },% Sao: http://chat.stackexchange.com/transcript/message/27874731#27874731, see
   also http://chat.stackexchange.com/transcript/message/27874722#27874722
                  }.
                 no edge,
               }{%
                  if={%
                    >{_O= _O< &}{1}{!parent.n children}{1}{!parent,parent.n children}%
                  \{% don't try to move if the node has more than 1 child or the grandparent has no more
   than that; otherwise, mark the node as one to move - we figure out where to move it later
                    proof tree toing,
507
                 }{no edge},
508
               }.
             }{no edge},
           }{},
         }{},
       },
       proof tree symud awto={% processed before typesetting nodes: if _this_ could be done during
514
   packing, that would be very nice, even if the previous stuff can't be
         if auto move={%
           proof tree aros'=0,
           for proof tree symud={%
             if proof tree toing={% this relies on an experimental feature of forest, which is anffodus
518
               for nodewalk={fake=parent,fake=sibling,descendants}{do dynamics},
               delay n={\foresteregister{proof tree aros}}{%
                 tempcounta/.max={>{0000w4+n}{level}{proof tree toing by}{proof tree toooing}{proof tree
    rhifo}{(##1+##2+##3)*##4}}{parent,sibling,descendants},
                  if tempcounta>=1{%
                    if={%
                      >{Rw1+n 00w2+n >}{tempcounta}{##1+1}{level}{proof tree toing by}{##1+##2}%
                    }{%
                      tempcounta-/.option=level,
                      tempcounta'+=1,
                     move by/.register=tempcounta,
528
                    }{no edge},
                 }{no edge},
               },
               proof tree aros'+=4,
             }{},
           },
534
         }{},
536
       },
       proof tree nodiadau={% processed after proof tree creu nodiadau and before before drawing tree:
537
   creates annotation content which may include cross-references, applies highlighting and additional
   TikZ keys to line numbers, justifications and to wffs where specified for entire proof lines
         where proof tree crefs={}{}{% resolve cross-refs in closures
538
           split option={proof tree crefs}{,}{proof tree rhif llinell cau},
           if content={}{%
540
             content/.option=proof tree rhestr rhifau llinellau cau,
541
           }{%
             content+/.process={_0}{\ }{proof tree rhestr rhifau llinellau cau},
543
           },
545
           typeset node,
         },
546
         if line numbering={% apply highlighting and additional TikZ keys to line numbers; initial
   alignment of numbers with proof lines
           for proof tree wffs={%
548
             if highlight line no={%
549
```

```
for name/.process={0w1000w3}{proof tree proof line no}{line no ##1}{proof tree proof line
    no}{line no options}{y}{% from Sao's anti-pgfmath version - rhaid ddweud proof tree proof line no yn
    ddwywaith ?! dim yn bosibl i ailddefnyddio'r gyntaf ?!
                 node options/.register=highlight format,
551
                 ##2.
                  y'=##3,
                 proof tree proof line no'=##1,
554
                  typeset node,
               }%
             }{%
               if line no options={}{%
558
                  if proof tree phantom={}{%
                    for name/.process={0w100w2}{proof tree proof line no}{line no ##1}{proof tree proof
   line no}{y}{%
                      v' = ##2.
561
                     proof tree proof line no'=##1,
562
                   }%
563
                 }.
564
               }{%
565
                  for name/.process={0w1000w3}{proof tree proof line no}{line no ##1}{proof tree proof
566
   line no}{line no options}{y}{%
                    ##2,
567
                    y'=##3,
568
                   proof tree proof line no'=##1,
569
                    typeset node,
570
                 7%
               },
572
             },
573
           },
         }{},
         if justifications={% initial alignment of justifications with proof lines, addition of content,
    resolution of cross-references and application of highlighting and additional TikZ keys
           for proof tree wffs={%
             if just={}{%
               if proof tree phantom={}{%
579
                  for name/.process={0w100w2}{proof tree proof line no}{just ##1}{proof tree proof line
580
   no}{y}{% from Sao's anti-pgfmath version - rhaid ddweud proof tree proof line no yn ddwywaith ?! dim
   yn bosibl i ailddefnyddio'r gyntaf ?!
                   y'=##2,
581
                   proof tree proof line no'=##1,
582
                 }%
583
               },
584
             }{% puts the content of the justifications into the empty justification nodes on the right;
585
    because this is done late, the nodes need to be typeset again
               if proof tree jrefs={}{}{% resolve cross-refs in justifications
586
                  split option={proof tree jrefs}{,}{proof tree rhif llinell},
587
                  if just refs left={%
588
                    +just/.process={0_}{proof tree rhestr rhifau llinellau}{\ },
589
                 }{%
590
                    just+/.process={_0}{\ }{proof tree rhestr rhifau llinellau},
                  },
               },
               if highlight just={% apply highlighting and additional TikZ keys to justifications, set
   content and merge any conflicting specifications, warning user if appropriate
                  for name/.process={0w10000w4}{proof tree proof line no}{just ##1}{proof tree proof line
    no}{just}{just options}{y}{% from Sao's anti-pgfmath version - rhaid ddweud proof tree proof line no
    yn ddwywaith ?! dim yn bosibl i ailddefnyddio'r gyntaf ?!
                    if={%
596
                     >{0_= 0_= |}{content}{}{content}{##2}%
                    }{% gweler isod - o gôd Sao
598
                      content={##2},
```

```
}{%
600
                      content+'={\foresteregister{merge delimiter}##2},
601
                      TeX={\PackageWarning{prooftrees}{Merging conflicting justifications for line ##1!
602
   Please examine the output carefully and use "move by" to move lines later in the proof if required.
   Details of how to do this are included in the documentation. } },
                    },
603
                    node options/.register=highlight format,
604
                    ##3,
                    y'=##4,
                    proof tree proof line no'=##1,
607
                    typeset node,
                  }% do NOT put a comma here!
                74%
610
                  for name/.process={0w10000w4}{proof tree proof line no}{just ##1}{proof tree proof line
611
    no}{just}{just options}{y}{% from Sao's anti-pgfmath version - rhaid ddweud proof tree proof line no
    yn ddwywaith ?! dim yn bosibl i ailddefnyddio'r gyntaf ?!
                    if={% from Sao's anti-pgfmath version - I appreciate this is faster, but why is it *
612
   required*?!
                     >{0_= 0_= |}{content}{}{content}{##2}%
613
614
                    }{%
                      content={##2},
615
                    }{%
616
                      content+'={\foresteregister{merge delimiter}##2},
617
                      TeX={\PackageWarning{prooftrees}{Merging conflicting justifications for line ##1!
618
   Please examine the output carefully and use "move by" to move lines later in the proof if required.
   Details of how to do this are included in the documentation.}},
                    Ъ.
619
                    ##3
620
                    y'=##4,
621
                    proof tree proof line no'=##1,
622
                    typeset node,
623
                  }% do NOT put a comma here!
624
                }
             },
           },
627
         }{},
628
         for proof tree wffs={% apply highlighting and TikZ keys which are specified for whole proof
629
   lines to all applicable wffs
           if proof tree phantom={}{%
             if highlight line={%
631
                for proof tree wffs/.process={00w2}{proof tree proof line no}{line options}{%
632
                  if proof tree proof line no={##1}{%
633
                    node options/.register=highlight format,
634
                    ##2,
635
                  }{}%
636
                }.
637
             }{%
638
                for proof tree wffs/.process={00w2}{proof tree proof line no}{line options}{%
639
                  if proof tree proof line no={##1}{##2}{},
640
                }.
641
             },
642
             delay={typeset node},
643
           },
644
         },
645
       },
646
       before packing={% initial alignment so we don't get proof line numbers incrementing due to
647
   varying height/depth of nodes, for example - when single branches is true and few nodes are grouped,
   this is also a reasonable first approximation
         for tree={%
648
           tier/.process={00w2+nw1}{level}{proof tree toing by}{##1+##2}{tier ##1},
649
         },
650
```

```
for root={% if there's no proof statement, adjust the alignment of the proof relative to the
651
   surrounding text
           if content={}{%
652
              !{n=1}.baseline,
653
           }{},
654
         }.
655
       },
656
       before computing xy={% adjust distance between levels for grouped nodes after tree is packed
657
         for tree={%
658
           if={%
659
            >{0 _0< &}{grouped}{1}{level}%
          }{% osgoi overlapping nodes, if posibl: cwestiwn https://tex.stackexchange.com/q/456254/
            not tempboola,
            tempcounta/.option=level,
663
            tempcountb/.option=proof tree toing,
664
            tempcountb+/.option=proof tree toooing,
665
            for nodewalk={fake=root, descendants}{if={> RO= On> O! O! OOw2+nR= &&&&
                 {tempcounta}{level} {!u.n children}{1} {proof tree arweinydd} {proof tree phantom} {
66'
   proof tree toing by} {proof tree toooing}{##1+##2} {tempcountb}
              }{tempboola}{}},
668
            if tempboola={}{l'=\baselineskip},
669
          }{},
670
         }.
671
       },
672
       before drawing tree={% set final alignment for proof lines which have been moved by effectively
673
   grouping lead nodes and moving their subtrees accordingly - this requires that each line number and
   justification be the child of the previous one and that if justifications are used at all, then
   justifications exist for all proof lines, even if empty
         if={>{RR|R!&}{line numbering}{justifications}{single branches}}{% correct the alignment of move
674
    by lines when single branches is false - o fersiwn anti-pgfmath Sao
           tempdimc'=0pt,% track cumulative adjustments to line numbers and justifications
675
           for proof tree cywiro symud={%
676
             if proof tree arweinydd={% only examine the lead nodes - their descendants need the same (
   cumulative) adjustments
               tempdima'/.option=y,
678
               if line numbering={% if there are line numbers, we use the previous line number's
679
   vertical position
                  for name/.process={0w1+nw1}{proof tree proof line no}{##1-1}{line no ##1}{% arafach ?
680
                    tempdimb'/.option=y,
681
                  }%
682
               }{% if not, we use the previous justification's vertical position
683
                  for name/.process={0w1+nw1}{proof tree proof line no}{##1-1}{just ##1}{% arafach ?
684
                    tempdimb'/.option=y,
685
                 }%
686
               },
687
               for parent={% the parent (which will be a phantom) gets aligned with the previous line
688
689
                 y'/.register=tempdimb,
               }.
690
               if tempdimb<={0pt}{% adjust so we align this line below the previous one (assuming we're
691
   going down)
                  tempdimb'-=\baselineskip,
692
               }{%
693
                  tempdimb'+=\baselineskip,
694
               },
               tempdimb'-/.register=tempdima,% how far are we moving?
               for tree={% adjust this node and all descendants
                    +/.register=tempdimb,
698
                 у
               }.
               tempdimb'-/.register=tempdimc,% deduct any tracked cumulative adjustments to line numbers
    and justifications
               if line numbering={% adjust the line numbers, if any
```

```
for name/.process={Ow1}{proof tree proof line no}{line no ##1}{%
702
703
                    for tree={%
                      y'+/.register=tempdimb,
704
                    },
                  }%
706
                }{},
                if justifications={% adjust the justifications, if any
708
                  for name/.process={0w1}{proof tree proof line no}{just ##1}{% t. 60 manual 2.1 rc1
                    for tree={%
710
                      y'+/.register=tempdimb,
711
                    }.
712
                  }%
713
                }{},
714
                tempdimc'/.register=tempdimb,% add the adjustment just implemented to the tracked
   cumulative adjustments for line numbers and/or justifications
             }{},
716
           },
         }{},
718
         if={%
719
            > RR| {auto move}{single branches}%
720
         }{}{%
721
           where proof tree arweinydd={%
722
723
             for nodewalk={%
                save append={proof tree walk}{%
724
                  current.
725
                  do until={%
726
                    > O+t_+t=! {content}{}%
727
                  }{parent}%
728
                }%
              }{},
730
           }{},
            where level>=1{%
              if grouped={%
                if in saved nodewalk={current}{proof tree walk}{}{%
734
                  no edge,
               },
             }{},
           }{},
738
         },
739
       },
740
     },
741
     move by/.style={% this implements both the automated moves prooftrees finds necessary and any
742
   additional moves requested by the user - more accurately, it implements initial moves, which may get
   corrected later (e.g. to avoid skipping numbers or creating empty proof lines, which we assume aren't
    wanted)
       if={
743
        >{_n<}{0}{#1}%
       }{% only try to move the node if the target line number exceeds the one i.e. the line number is
745
   to be positively incremented
         proof tree cadw toing by/.option=proof tree toing by,
746
         proof tree arweinydd,
747
         for tree={%
748
            if={%
749
            >{_n<}{1}{#1}%
           }{% track skipped lines for which we won't be creating phantom nodes
             proof tree toing by+=#1-2,
             proof tree toooing'+=1,
753
           }{},
         },
         delay={%
756
           replace by={% insert our first phantom
757
```

[, 758 if={% 759 $\{_n < \{1\} \{\#1\} \}$ 760 }{% 761 child anchor=parent, 762 parent anchor=parent, 763 }{% 764 child anchor=children, parent anchor=children, 766 }, proof tree phantom, 768 edge path/.option=!last dynamic node.edge path,% Sao ivanovi: http://chat.stackexchange. 769 com/transcript/message/27990955#27990955 edge/.option=!last dynamic node.edge, append, before drawing tree={% 772 if={>{RR|}{line numbering}{justifications}}{% proof tree proof line no/.process={0w1+n}{!parent.proof tree proof line no}{##1+1}, 774 }{}, }, 776 if={% 777 >{_n<}{1}{#1}% 778 }{% if we are moving by more than 1, we insert a second phantom so that a node with 779 siblings which is moved a long way will not get a unidirectional edge but an edge which looks similar to others in the tree (by default, sloping down a line or so and then plummeting straight down rather than a sharply-angled steep descent) delay={% 780 append={% 781 [, 782 child anchor=parent, 783 parent anchor=parent, 784 proof tree toing by=#1-2+proof_tree_cadw_toing_by, 785 786 proof tree phantom, 787 edge path/.option=!u.edge path, edge/.option=!u.edge, 788 before drawing tree={% 789 if={>{RR|}{line numbering}{justifications}}{% 790 proof tree proof line no/.process={Ow1+n}{!n=1.proof tree proof line no 791 $\{\#\#1-1\},\$ }{}, 792 }, 793 append=!sibling, 794]% 795 796 }, }, 797 }{% 798 if single branches={}{% 799 delay={% 800 for children={% 801 no edge, 802 }. 803 }, 804 }, 805 }, 806]% 807 }, 808 }, 809 }{% 810 TeX/.process={0w1}{name}{\PackageWarning{prooftrees}{Line not moved! I can only move things 811 later in the proof. Please see the documentation for details. ##1}},

812

},

```
Ъ.
813
     proof tree cref/.style={% get the names of nodes cross-referenced in closure annotations for use
814
   later
       proof tree crefs+/.option=#1.name,
815
     Ъ.
816
     proof tree rhif llinell cau/.style={% get the proof line numbers of the cross-referenced nodes in
817
   closure annotations, using the list of names created earlier
       if proof tree rhestr rhifau llinellau cau={}{}{%
818
         proof tree rhestr rhifau llinellau cau+={,\,},
819
       },
820
       proof tree rhestr rhifau llinellau cau+/.option=#1.proof tree proof line no,
821
     Ъ.
822
     proof tree jref/.style={% get the names of nodes cross-referenced in justifications for use later
823
       proof tree jrefs+/.option=#1.name,
824
     Ъ.
825
     proof tree rhif llinell/.style={% get the proof line numbers of the cross-referenced nodes in
826
   justifications, using the list of names created earlier
       if proof tree rhestr rhifau llinellau={}{}{%
827
         proof tree rhestr rhifau llinellau+={,\,},
828
       },
829
       proof tree rhestr rhifau llinellau+/.option=#1.proof tree proof line no,% works according to Sao'
830
   s anti-pgfmath version
     Ъ.
831
     line no override/.style={% 2018-02-19 ateb https://tex.stackexchange.com/a/416037/
832
       before drawing tree={
833
         for name/.process={Ow}{proof tree proof line no}{line no ##1}{
834
           content=\linenumberstyle{#1},
835
            typeset node,
836
         },
837
       },
838
     },
839
     no line no/.style={% 2018-02-19 gweler uchod
840
841
       before drawing tree={
         for name/.process={Ow}{proof tree proof line no}{line no ##1}{
842
843
            content=.
            typeset node,
844
         },
845
       },
846
     Ъ.
847
     proof tree dadfygio/.style={% style for use in debugging moves which displays information about
848
   nodes in the tree
       before packing={%
849
         for tree={%
850
            label/.process={000w3}{level}{proof tree toing by}{id}{[red,font=\tiny,inner sep=0pt,outer
851
   sep=0pt, anchor=south]below:##1/##2/##3},
852
         },
       },
853
       before drawing tree={%
854
         for tree={%
855
            delay={%
856
              tikz+/.process={0w1}{proof tree proof line no}{\node [anchor=west, font=\tiny, text=blue,
857
   inner sep=0pt] at (.east) {##1}; },
858
            }.
         },
859
       },
860
     },
861
     proof tree alino/.style={% debugging / dangos dimension stuff
862
       before drawing tree={%
863
         tikz+/.process={%
864
            RRRRw4{proof tree inner proof midpoint}{line no width}{line no dist}{just dist}
865
            ſ
866
```

```
\begin{scope}[densely dashed]
867
                \draw [darkgray] (##1,0) coordinate (a) -- (a |- current bounding box.south);
868
                \draw [green] (current bounding box.west) -- ++(##2,0) coordinate (b);
869
                \draw [blue] (b) -- ++(##3,0) coordinate (c);
870
                \draw [magenta] (c) -- ++(##4,0);
871
              \end{scope}
872
           }%
873
         }.
874
       },
875
     },
876
   3
877
   % \environbodyname\prooftreebody
878
   \bracketset{action character=@}
879
880 \NewDocumentEnvironment{\prooftrees@enw}{ m +b }{% \forest/\endforest from egreg's answer at http://
   tex.stackexchange.com/a/229608/
     \forest
881
        (%
882
         stages={% customised definition of stages - we don't use any custom stages, but we do use
883
   several custom keylists, where the processing order of these is critical
           for root'={% nothing is removed from the standard forest definition - we only change it by
884
   adding to it
             process keylist register=default preamble,
885
             process keylist register=preamble,
886
           },
887
           process keylist=given options,
888
           process keylist=before typesetting nodes,
889
           % first two additions: process two custom keylists after before typesetting nodes and before
890
   typesetting nodes
           process keylist=proof tree ffurf,
891
           process keylist=proof tree symud awto,
892
           typeset nodes stage,
893
           process keylist=before packing,
894
           pack stage,
896
           process keylist=before computing xy,
897
           compute xy stage,
           % second two additions: process two custom keylists after computing xy and before before
898
   drawing tree
           process keylist=proof tree creu nodiadau,
899
           process keylist=proof tree nodiadau,
900
           process keylist=before drawing tree,
901
           draw tree stage,
902
         },
903
       )%
904
       proof tree,% apply the proof tree style, which sets keylists from both forest's defaults and our
905
   custom additions
       #1,% insert user's preamble, empty or otherwise - this allows the user both to override our
906
   defaults (e.g. by setting a non-empty proof statement or a custom format for line numbers) and to
   customise the tree using forest's facilities in the usual way - BUT customisations of the latter kind
    may or may not be effective, may or may not have undesirable - not to say chaotic - consequences,
   and may or may not cause compilation failures (structural changes, in particular, should be avoided
   completelv)
       [, name=proof statement @#2]%
907
     \endforest
908
   }{}
909
910
   \ExplSyntaxOn
911
   \cs_new_protected_nopar:Npn \__prooftrees_memoize:n #1
912
913 {
     \mmzset{
914
       auto = { #1 } { memoize },
915
     }
916
```

```
917 }
918 \cs_generate_variant:Nn \__prooftrees_memoize:n { V }
919 \hook_gput_code:nnn { begindocument / before } { . }
920 {% paid â memoize bussproofs prooftree ...
921 \@ifpackageloaded{memoize}{
922 \__prooftrees_memoize:V \prooftrees@enw
923 }{}
924 }
925 \ExplSyntaxOff
926
927 \endinput
```

928 %% end prooftrees.sty